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Report 2262

CORRELATION STUDY OF LABORATORY PHYSICAL AND CHEMICAL DATA WITH DYNAMOMETER ENGINE SEQUENCE PERFORMANCE TESTING OF ENGINE LUBRICATING OILS

by
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December 1978

December 1978

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U.S. ARMY MOBILITY EQUIPMENT
RESEARCH AND DEVELOPMENT COMMAND
FORT BELVOIR, VIRGINIA

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REPORT DOCUMENTA		READ INSTRUCTIONS BEFORE COMPLETING FORM
I. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
2262 🗸		
A. TITLE (and Sublitio) CORRELATION STUDY OF LABO AND CHEMICAL DATA WITH DYS SEQUENCE PERFORMANCE TEST LUBRICATING OILS	NAMOMETER ENGINE	5. Type of Report a Period Covered Technical Report Sept 1977 thru Sept 1978 6. Performing org. Report number
Maryland D. Kemp Francis E. Council, Jr.		6. CONTRACT OR GRANT NUMBER(*)
Performing organization name and at Fuels & Lubricants Division, Energy Laboratory, US Army Mobility Equi Development Command, Fort Belvo	& Water Resources ipment Research and bir, Virginia 22060	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS A8H20EL0221
US Army Mobility Equipment Research Command; ATTN: DRDME-GL Fort Belvoir, Virginia 22060	arch and Development	12. REPORT DATE December 1978 13. NUMBER OF PAGES 136
14. MONITORING AGENCY NAME & ADDRESS/II	different from Controlling Office)	15. SECURITY CLASS. (of this report)
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SUMMARY

In this study, many tests on lubricating oils have been considered collectively and not as separate tests, and comments are made on the significance of the data with particular reference to the correlations among the data. Normally, an assessment of the significance of a test is accomplished by examining the correlation of the test with performance, i.e., deciding whether a change in the performance of an oil will be predicted by a change in a laboratory test result. In this report, the significance of a test is assessed by considering its relationship with other tests and not from a consideration of performance data. Performance data of the quality and quantity desired are not presently available.

The tests considered include some of the common inspection tests usually employed to characterize physical and chemical properties of the oils. The data was retrieved from the Laboratory files. Twenty-six pieces of analytical data were collected but because of the lack of data on all the samples, 13 items were finally chosen for the study. The items included analytical results for gravity; flash point; viscosity at 210°F, 100°F, and 0°F; viscosity index; pour point; total acid number; carbon; sulphur; sulphated ash; phosphorus; and calcium.

Three statistical techniques have been used to analyze the data and to examine the interdependence of these tests. The first task of the analysis is to determine the basic distributional characteristics (descriptive statistics) of each of the variables to be used in the subsequent statistical analysis. Information on the distribution, variability, and central tendencies of the variables provides necessary information required for selection of subsequent statistical techniques and constitutes a basic computer reference document for the entire data file. The mean, for example, provides a measure of central tendency; standard deviation and variance indicate the degree of dispersion around the mean, and measures such as skewness and Kurtosis allow one to more precisely define the shape of the variables' distribution.

The analysis of the descriptive data shows a considerable amount of variance — the data does not cluster around the mean. The standard deviation shows large values for the standard deviation. The skewness, which takes a value of zero when distribution is a symmetric bell-shaped curve, and a plot of the data for gravity show departure from a normal distribution. The Kurtosis further shows departure from a normal distribution. A positive value for kurtosis shows a peaked (narrow) distribution. A negative value shows a flatter distribution. Both positive and negative values exist for Kurtosis with positive values (narrow) predominating. Conclusive deductions cannot be made from the descriptive statistics.

The distinctive characteristic of factor analysis is its data-reduction capability. Once an array of correlation coefficients is obtained for a set of variables, factor analysis enables one to see whether some underlying pattern of relationships exist such that the data may be arranged or reduced to a smaller set of factors or components that may be taken as source variables accounting for the observed interrelations in the data. The results of the factor analysis show that, of the total variance in the data, 85% of the total variance registered for the 13 elemental pieces of data is accounted for by the first four factors, G, FL, Viscosity (210°F, 10°F, 0°F, VI), and TAN. This suggests that a relationship between these four factors will define performance parameters of the lubrication oils. Although individual parameters such as CRAM and SAH (.7709), CRAM and CA (.2167), and SAH and CA (.8679) show good dual correlations, their effects on the total variance are small (a correlation of 1.0 is perfect correlation).

Principal component analysis was employed to study the overall relationship of groups of tests, and some use was made of correlation coefficients and Pearson's product moment correlations. Principal component analysis is used to evaluate components which are linear combinations of the original tests, and the analysis shows how many independent properties are being measured by the test considered. All the solutions employed previously extract orthogonal factors for the matrix in order of their importance. The first factor, say gravity, greatly affects (loads) on all other factors. In the principal-component matrix, the variables are in turn rotated and the data is presented in graphical form. Each possible pair of factors, including all the 13 items of data considered, is orthogonally rotated. From the rotation, one obtains overall relationship of groups of data. For example, employing gravity 2 as the horizontal factor and flash point 2 as the vertical factor, elements 8, 9, and 12 form a separate group to elements 2, 10, 7, 13, and 3. That is, flash point, sulphur, total acid number, pour point, and viscosity (2, 10, 7, 13, 3) all react to one property of the lubricating oil while carbon, sulphurated ash, and calcium (8, 9, 12) react to another property. Similar applications can be made with other plots, and when dynamometer and field performance data are included, information relating the three (lab data, dynamometer data, performance data) should evolve.

Further study along these lines is indicated.

PREFACE

The inspiration and motivation for this work came from Mr. Maurice E. LePera, Chief, Fuels & Lubricants Division, under whose general supervision the tests were performed.

The work was performed under Mission Account No. A8H20EL0221.

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ABBREVIATIONS

G = Gravity, API FL = Flash Point

 V_{210} = Viscosity @ 210° F V_{100} = Viscosity @ 100° F

V₀ AP = Viscosity @ 0°F (Apparent) V₀ EX = Viscosity @ 0°F (Extrapolated) V₋₂₀ = Viscosity @ -20°F (Extrapolated)

VI = Viscosity Index (Calculated)

pp = Pour Point

stpp = Stable Pour Point
TBN = Total Base Number
TBNN = Total Base Number
TAN = Total Acid Number

CRAM = Ramsbottom Carbon Residue

SAH = Sulphated Ash Residue

S = Sulphur P = Phosphorus

CA Calcium (Additive) Ba Barium (Additive) Zn Zinc (Additive) NA Sodium (Additive) K Potassium (Additive) N Nitrogen (Additive) Mg Magnesium (Additive) B Boron (Additive)

Other = To include wear and contaminant materials.

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CORRELATION STUDY OF LABORATORY PHYSICAL AND CHEMICAL DATA WITH DYNAMOMETER ENGINE SEQUENCE PERFORMANCE TESTING OF ENGINE LUBRICATING OIL

I. INTRODUCTION

A lubricant serves a multitude of functions in many mechanical systems among which are the following: (1) prevention of friction and wear, (2) removal of heat from the lubricant-engine system, (3) removal of contaminants and debris from the lubricant-engine system, (4) transmission of power in hydraulic systems, and (5) prevention of metallic corrosion in the lubricant-engine system. At the same time, the lubricant must be compatible with a variety of gaskets and elastomers employed to seal lubricant-engine systems to protect them from the elements.

It has been established and adequately documented that the lubricants required by the sophisticated mechanical system and power plants of today cannot be formulated by simple base stocks and additives. Lubricants used today are complex mixtures of base stocks incorporating a combination of chemical additives to achieve the desired performance characteristics. In addition to base stocks, lubricants contain additives designed to effect:

oxidation inhibition
cleansing action — detergents
dispersing action — dispersants
counteraction of extreme pressure
corrosion inhibition
depression of pour point
improved viscosity
rust inhibition
chatter prevention
squawk prevention
foam prevention
gelling
thickening

At the same time, lubricants must remain homogeneous over broad temperature ranges.

In order to insure that lubricating oils meet these stringent requirements as are appropriate, a number of laboratory physical and chemical tests are performed for characterization, quality control purposes, and evaluation. The laboratory tests include measurements of viscosity, specific gravity, flash point, calcium, sodium, barium, zinc, potassium, carbon, nitrogen, magnesium, sulphur, ash, base number/acid number, pour point, and boron.

In addition to the laboratory physical and chemical tests performed on candidate lubricating oils, engine dynamometer, multicylinder sequence tests are also performed to evaluate engine oils. These tests are designed to evaluate tendencies toward rusting, wearing, oxidation (stability), ring sticking, corrosive tendency, and accumulation of deposits both in the crankcase and on the surface of the mechanical parts.

The purpose of the work reported herein is to seek correlations between the laboratory physical and chemical test data and the performance of lubricating oils in the dynamometer sequence tests, to examine the interdependence of the tests, and from the results to comment on the significance of the tests.

II. BACKGROUND

A number of studies have been made on lubricating oil base stocks, and meaningful relationships have been established between certain measurable properties. The relationship between thermal properties and inspection tests was reviewed by Cragoe¹ in 1929. Physical properties and chemical composition were summarized by Van Nes and Van Westen² and Waterman.³ Van Nes and Van Westen showed that %C_A, %C_N, ${}^{\prime\prime}C_{P}$, R_{T} , R_{A} , and R_{N}^{-4} could be calculated from the refractive index, density, and molecular weight. These chemical properties have originally been determined using elemental chemical analyses, thus illustrating the interdependence of the chemical analyses and the inspection tests. Waterman described a similar method of carbon-type analysis using measurements of viscosity, refractive index, and density and reported correlations of ultrasonic viscosity and surface tension, Faraday effect, and parachor with other physical constants and the chemical composition.

When large numbers of tests are available for the characterization of a material, it is generally realized that many of the tests are interrelated, and some of these relationships may be known. The relationships among specific groups of tests can be readily established by using the statistical technique known as regression analysis. What is not generally known is how many truly independent properties are being measured by any group of tests.

C. S. Cragoe, "Thermal Properties of Petroleum Products," N. B. S. Publication # 97 (1929).

K. Van Nes and H. A. Van Westen, "Aspects of the Constitution of Mineral Oils," Amsterdam; Elsevier (1951).

H. I. Waterman, "Correlation Between Physical Constants and Chemical Structure," Elsevier (1958), p. 11; Anal. Chem. Actor (1958), 18, p.5

[%]CA: Percentage carbon in aromatic ring.

 ⁽RCN): Percentage carbon in naphthenic ring.
 (RCP): Percentage carbon not in ring structures.

R_T: Number of rings per molecule.

Number of aromatic rings per average molecule.

Number of naphthenic rings per average molecule.

This initial study of lubricating oils had several goals. One was to obtain some base-line values of any randomly selected group of oils such that any particular oil could be compared with the group as a whole. Another goal was to see if there were any relationships among the various chemical properties of oils which could be exploited in such a way as to achieve a better understanding of the properties of a lubricating oil which make for a better lubrication. A third goal was to see what relationships existed for the various oils such that, hopefully, some of the tests performed on oils could be determined as redundant.

III. EXPERIMENTAL AND ANALYTICAL PROCEDURES

The 80 lubricating oils studied included preparations from a variety of base stocks. In addition, the additives employed were from a variety of suppliers and were not individually characterized.

The results of the chemical analysis of 80 lubricating oils were obtained from the files of the Fuels and Lubricating Division.

The properties of the 80 samples taken for the study are shown in Table 1. The samples were identified simply by number, and the test results were taken randomly from oil samples submitted for approval under Specification MIL-L-2104. The test results were taken from an variety of laboratories certified to perform the tests. A tabulation of the physical and chemical properties of an oil can assist the user and the oil refiner in defining a consistently uniform product. While the physical and chemical properties of an oil (discussed in this report) do not in themselves define oil performance, these individual oil properties are meaningful and are related to the ability of the oil to fulfill its function as a lubricant. Crude petroleum oils have as principal components three basic types of hydrocarbon molecules, i.e., paraffinic, naphthenic, and aromatic. The types of molecules that predominate are a basis for the classification of oils. Crude oils are typified as belonging to one of four classes: paraffinic, naphthenic, asphaltic, and mixed base. In the paraffinic type, paraffinic hydrocarbons predominate; in the naphthenic type, naphthenic hydrocarbons predominate; in the asphaltic type, naphthenic and aromatic hydrocarbons exist together; and in the mixed type, paraffinic, naphthenic, and aromatic types exist together. Crude oils as they come from the ground can be mixtures of gaseous products, gasolines, diesel fuels, lubricating oil stocks, asphalt, etc. The various classes of products are separated primarily through distillation. Precipitation of the heaviest viscous fractions using a solvent is also practiced. The lubricating oil fractions resulting therefrom provide a series of base stocks of varying volatility and viscosity. These base stocks are referred to as neutral fractions and bright stock. These fractions generally require further refining plus the addition of additives to make them suitable for engage oil applications. The complete chemical and physical data collected on engine oils is

Table 1. Properties of 80 Lubricating Oils Selected for Study

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CRAM	1.20	1.45	96		1.20	500	1.00	1114	1.49	1.21	1139	1.02		1.68	. 4	175	1.10	1.70	1.14	1.00		1 1 0	1.27	1.66	1.54	1.35	961	1.0.1		7.63	1	1.45	1.55	1.75	1.54
TAN	1.6	•	3.6	2.5	5.6	1		1.8	2.0	2.7	3.5	1.9	2,3	7.3	3.6	2.5	2.4	2.8	1.8	2.6	· .		1.9	2.4	2.2	2.0	7.7		543		200		5.9	4.1	
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1.00	1.00	1.48	96.	.91	450	.98	98	1.60	1.55	96.	1.62	.93	.91	. 85	1,25	1.07	• 95	06.	16.	.91	-26.	1.51	1.68	.95	1.07	. 98	1.51	96.	1.50	1.65	1.74	16.	1.60	1.00	38
1.28	1.29	-	=	4	4	1.24		1.56			104	1.1	-	1.1		.7	1.4	1.10	1,10	1.14	7	1.49	1072	1.10	1,	1.10	1.47	1.12	117	1.50	2.00	1.10	1.55	1.10	115
2.2	2.5	4 .	-	5.4	_	3.1		2.0	2.1	•	4		-		2.1	2.5		2.4	2.08	2.3	2.B	2.0	204	1.8	•	2.7	2.2	1.6	205	10.0	2.8	2.8	2.4	2.3	22
91.0	95.0	4 .	4	90.0	86-7	100.0	100.0	69.7	99.0	102.0	93.0	ე•ე6	90.0	97.0	101,0	0.66	100,1	0.06	94.	162.0	94.0	0.46	4	100.0	-	0.76	100.00	100.0	97.0	95.0	9.96	0.46	95.0	91.0	93.0
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12.83	12.21		7		4		•	•	•	10.50	4	11.67	4		3	۲.	11.60	12.40	11.36	11.76	11.36		12.30	12,30	12,18	9.	-	2	7	12.57	11,85		12,30		12.88
476.0	425.0		44500	145.0	g	450.0	S	4.70.0	460.0	7.044	44500	9	44500	460.0	465.0	460.0	450.0	445.0	455.0	450.0	455.0	475.0	450 0	480.0	9	480.0	0.064	475.0	487.0	0.444	455.0	5	5.5.0	450.0	480.0
25.60	25.80	200	7	5.0	3	0.9	6	2.5	5	28.20	3	5.3	25.63	25.60	6.1	26.70	28.50	25.00	7.07		1.1	5	300	28.50	9	2.	25.89	28.30	22.60	23.50	26.53	27.73		•	25.80

shown in Table 2 and includes 26 pieces of information. Due to the lack of complete results on all 80 samples, 13 items of information have been selected for these studies. They are shown in Table 3.

The initiation of this study includes a plot of a typical set of test results (Gravity, G) as shown in Figure 1 and a presentation of the gravity test measurement in distribution form as shown in Figure 2.

An initial statistical survey of these oils, those with a sufficiently large data set, was performed using the Statistical Package for the Social Sciences (SPSS)⁵ and a CDC computer. These are summarized in Table 3. They include the mean, variance, range, standard error, Kurtosis, maximum, minimum, skewness, and standard deviation where Kurtosis = measure of relative peakedness or flatness of curve defined by the distribution of cases. (A normal distribution will have a Kurtosis of zero.) When the Kurtosis is positive, then the distribution is more peaked (narrow) than it would be for a normal distribution while a negative value means that it is flatter:

Kurtosis =
$$\frac{\sum_{i=1}^{N} [(X_i - \bar{X})/S]^4}{N}$$

The computing formula used by SPSS is:

Kurtosis =
$$\frac{\left\{ \left[\sum_{i=1}^{N} X_{i}^{4} - 4\overline{X} \left(\sum_{i=1}^{N} X_{i}^{3} \right) + 6\overline{X}^{2} / \sum_{i=1}^{N} X_{i}^{2} - 4\overline{X}^{3} \left(\sum_{i=1}^{N} X_{i} \right) \right] / N \right\} + \overline{X}^{4} - 3}{\left\{ \left[\left(\sum_{i=1}^{N} X_{i}^{2} \right) - N\overline{X}^{2} \right] / (N-1) \right\}^{2}}$$

In looking at the Kurtosis of the data as it related to individual parameters, it is seen that the data for individual sets do not fall together. Kurtosis measures the degree of peakedness exhibited in individual sets of data, and a Kurtosis of zero corresponds to a normal distribution. Large, positive values indicate more peakedness (narrow) than for a normal distribution. Negative values mean a curve flatter than normal distribution. In the data collected in these tests, it is seen that for G, the API gravity; FL, the flash point; SAH, sulphated ash residue; and CA, calcium, the value of Kurtosis is approaching that of a normal distribution — a value less than 1. Values less than 5 and more than 1 can be assigned to only four additionally measured parameters: pp. pour point; CRAM, Ramsbottom Carbon; VI, Viscosity Index; and V 100, Viscosity 100°F.

Norman H. Nir, C. Hadlai Hull, Jean G. Jenkins, Karin Steinbrenner, and Dale H. Bent, Statistical Package for the Social Sciences. 2nd Edition, McGraw Hill Book Company, New York.

Table 2. Complete Chemical and Physical Data on Engine Oils

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Table 2. Complete Chemical and Physical Data on Engine Oils (Cont'd)	VI PP SIPP TON TON CRAM SAIL S P (A BA ZN NA K N M). B	00.0 10.0 410.0.1 0.0 410. 5999. 435. 591. 084. 85. 45.1 01.5 9.99 0.00 0.001.6	100.00 0.00 0.00 0.00 0.00 0.00 0.00 0.	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nical an	415	9 99.9	0 00 00	0 0 00 00	0 0 00 00	0 00 00	6 66 60	6 6.66 00			6 6.66 00	8.56	6 6.86 00	6 6.66 00			56 6.66 00	6 6.66 00	- 1		88.3	8.86	88.66	8.66	99.3	8.86		8.66	6 8766 00	
ete Chen	2	0 0.00	01.0	0 0 0	9- 0- 00	0 20	93.0	90.0	99.0	97.4 -5.	.01.0	99.0 -5.	. 03.0 -5.	91.0	94.0 -5.	.02.0 -5.	34.0 -5.	90 -10.	.01.0 6.	63.0	99.0 -5.	0. 76	0 0 0	.6- 0.00	97.0		95.6 -5.		25.6 -5.	
Comple	V15.20	6.8686 0	6.999.9	6 6666 9	6.0000	0 9996 0	6.6666 1	6 6666 6	6.5655 8	6.8686 0	6. 99 99 . 9	6 . 56 56 9	6 3399.9	6.8666 0	6. 6666 0	6.8686 3	6.6666 3	6.6666 0	6.6686 0	6 3839.9	6 66666 3	5.6666	6. 99 99.9	6.6666 0	9 999.9	6. 6666 0	6 9999.9	6.6666 0	6 3939.5	
Table 2.	Voex	9 15094.	3.9 15094.	. 9 18000	9.9 17699.	9000	.9 15300	3.9 93999.	9.9 21500.	3.9 15666.	9.9 14568.	99999.9 15380.	9.9 127.46.	9.9 215.0.	99999.9 15360.	111.32 99999.9 14110.	9.9 15300.	99999.9 17511.	39999.9 14000.	9.9 14500.	15:55.	3 17 500.	3 15000.	9.9 14700.	3.9 45500.	9.9 17000.	3.9 12000.	3.9 15301.	. 16486 8.5	
1	IOO VOAP	6.64 99999.	3.60 9999	7.91 9999	3.00 9999	10 9999	5.86 9999	2.43 9999	33.95 99999.	1.57 99999.9	6666 14.0	5666 06 .	1,00 99999	3.95 99999.	3, 60 9999	1.32 9999	3, 85 9999	6666 61.0	6 666 00 9	1.20 99999.	. 4 99999.9	4.64 9999.	1.50 99999.	. 46 6666 04. 0	8 26 3399	1.00 99999.9	1.66 9999	1.60 99999.	7.01 9999	16000 05 3
	N210 V	12.45 12	12.45 12	11.34 11	12,35 12	10.56	11.53 111	**	••	12.12 12	12, 13 12	14.18 14	11.61.11	-:	1		11.36 11			25.50		20.00	25.67.25	14.62 12	12. 12.51	12.57 13	11,05 11	11.36 11	12.31 12	11 37 12
	7.4	.00 450.1	MC4.04 25.07 450.0 12.45	MC0181 25.20 470.0 11.34	.10 650.5	.20 446.3	0.644 04.	ACC102 25.30 465.0 11.67	MCU161 25.00 445.9 12.40	MC0319 25.60 460.0 12.12	465.	490.	F. 1221 28.50 450.0 11.6	MCL245 25.00 445.0 12.4	#C0246 27.70 455.0 11.35	#CL117 27.96 456.0 11.76	MC6172 27.70 455.0	MCUC73 25.60 475.0 12.6	T.0178 28.50 450.3			2000 00 00 00 000	200 496.0	. 574 00.	7,0153 27.50 450.0	# 12.57 12.57 444.0 12.57	15: 455.0	.70 455.0	5: 5	
	DENT C	MCU182 26.00 450.3 12.4	PC 1014 25	MC0181 25	MC0136 25,10 450,0 12,35	MCL199 28.20 446.0 10.50	PC0011 24.49	ACC102 25	MC4161 25	MC8 518 25	- 4. 3277 26.17 455.0 12.13	400140 69	F. 1221 21	MC1245 25	M	ACL117 27	MC6172 27	MCDETA 65	-CU178 28	2000 200 200 200 200 200 200 200 200 20	MC 7007 20	200000	T. 0.301 (2) 60 491.0 12.75	T. U.SC. C8. 30 4/5. U 12. C2	Part 53 67	FC 1239 23	65,50 455,0 11,05	42.171 27.70 455.0 11.36	1. 34 Co. 41 5. 5. 1 . 2. 31	99 6 19 19

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Table 3. Statistical Survey of 13 Engine Oil Samples

MEAN	26.523	SID ERR	.127	STD DEV	1.13
VARIANCE	1.287	<pre></pre>	.271	SKEWNESS	31
RANGE	5.600	MINIMUM	23.166	MUMIXAM	29.600
VALID CASES	85	MISSING C	ASES :		
VARIABLE FL					
	462.150	STO ERR	1.972	STD DEV	17.634
	311.965	KURTOSIS	239	SKENNESS	. 20
RANGE	80.600	MINIMUM	425.00	MUMIXAM	505.000
VALID CASES	50	MISSING C	ASES i		
VARIABLE V210	0				
MEAN	12,121	STO ERR	.393	STO DEV	. 633
VARIANCE	.694	KURTOSIS	19.488	SKENNESS	2.53
RANGE	7.250	MINIMUM	10.190	HLHIXAM	17.34
VALID CASES	50	MISSING C	ASES)		
VARIABLE V ₁₀₀) d				
MEAN	120.172	STD ERR	1.263	STD DEV	11.299
VARIANCE	127.567	KURTOSIS	2.193	SKENNESS	27
RANGE	68.890	MINIMUM	87.610	MUMIXAM	156.500
VALID CASES	80	MISSING C	ASES U		
VARIABLE VoE	X				
MEAN 18	320.607	STO ERR	1871.409	STD DEV	16738.393
VARIANCE . 2	301E+09	KURTOSIS	20.140	SKENNESS	4.497
RANGE 94	599,900	MINIMUM	5460.000	MUNIXAM	99999.900
VALID CASES	80	MISSING CA	ISES 0		
VARIABLE VI					
MEAN	97.695	STO ERR	.641	STD DEV	5.732
VARIANCE	32.855	CURTOSIS	1.866	SKENNESS	683
RANGE	32.000	HINIHUH	78.206	MUMIXAM	110.000
VALID CASES	80	MISSING CA	SES 0		
VARIABLE TAN					
MEAN	2.396	STD ERR	.577	STD DEV	.693
VARIANCE	. 480	KURTOSIS	17.966	SKENNESS	3.171
RANGE	5.200	MUNIMUM	1.564	MAXIMUM	6.700
VALID CASES	80	MISSING CA	SES .		

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Table 3. Statistical Survey of 13 Engine Oil Samples (Cont'd)

VARIABLE CR		1 Survey of 13 F		•	
MEAN	1.290	610 600			
VARIANCE	.086	STD ERR CURTOSIS	.333	STD DEV	.293
RANGE	1.560	MINIMUM	1.125	SKENNESS	. 761
NAMOC.	1.960	HINIHOR	.750	MAXIMUM	2,310
VALID CASES	36	MISSING CA	SES 0		
VARIABLE SA					
MEAN	1.281	STO ERR	.(38	STO DEV	, 336
VARIANCE	.113	KURTOSIS	.114	SKEWNESS	.772
RANGE	1,520	MINIMUM	. 853	HLHIXAH	2.370
VALIO CASES		MISSING CA	SES (
VARIABLE S					
MEAN	.760	STD ERR	• : 98	STD DEV	477
VARIANCE	.768	KURTOSIS	55.711	SKEWNESS	.877
RANGE	7.610	MUNIMUM	.250	MAXIMUM	6.869 7.860
VALID CASES	80	MISSING CA	SES C		
VARIABLE P					
MEAN	.098	SID ERR	.(10	SIO DEV	110
VARIANCE	.008	KURTOSIS	72.654	SKENNESS	
RANGE	258.	MINIMUM	.650	MAXIMUM	8.340
VALID CASES	80	MISSING CAS	SES 0		
VARIABLE CA					
MEAN	.300	STO ERR	.:15	STD DEV	.131
VARIANCE	.317	<urtosis< td=""><td> 363</td><td>SKEWNESS</td><td>001</td></urtosis<>	363	SKEWNESS	001
RANGE	.632	MINIMUM	18	MAXIMUM	650
VALID CASES	80	MISSING CAS	SES 0		
VARIABLE PP					
MEAN	-4.487	STO ERR	.638	570.054	
VARIANCE	32.531	KURTOSIS	3.679	STO DEV	5.704
RANGE	25.0:0	MINIMUM	-25.000	SKEWNESS	-1.630
VALIO CASES	80	MISSING CAS			

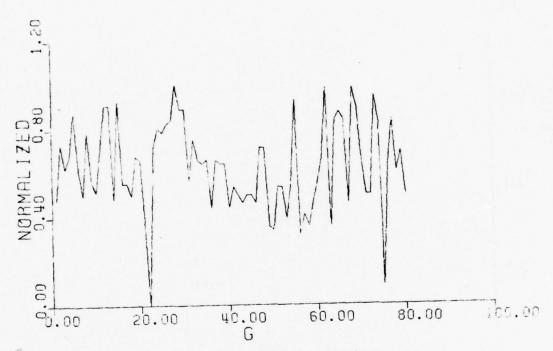


Figure 1. Plot of a typical set of test results.

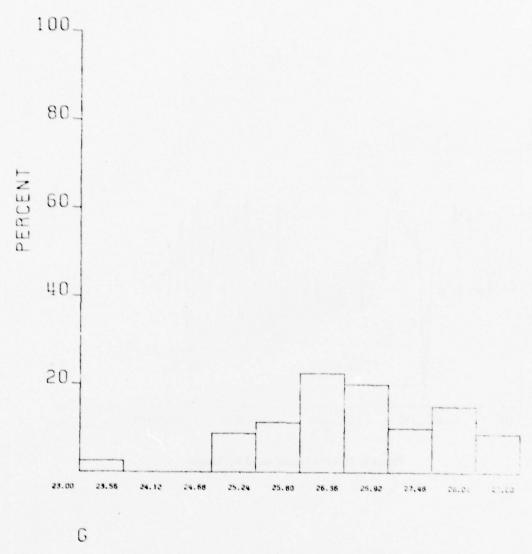


Figure 2. Gravity test measurement in distribution form.

The Kurtosis values measure the grouping of the values for individually measured properties:

"Mean" is the most common measure of central tendency for variables measured at the interval level:

$$X = mean = \frac{\sum_{i=1}^{N} X_i}{N}.$$

"Variance" measures dispersion of data about the mean of the interval-level variable. This statistic is one way of measuring how closely the individual scores on the variable cluster around the mean. Mathematically, it is the average squared deviation from the mean:

$$s^2 = \frac{\sum_{i=1}^{N} (X_i - \overline{X})^2}{N-1}.$$

Squaring the deviations from the mean considers all differences from the mean both positive and negative, and it gives additional weight to extreme cases. The variance will be small when there is a great deal of homogeneity in the data; for, then, most cases will have very small deviations from the mean.

"Skewness" is a statistic used to determine the extent to which a distribution of cases fits or approximates a normal curve since it measures deviations from symmetry. Skewness takes a value of zero when the distribution is a complete, symmetric, bell-shaped curve. A positive value indicates that the cases are clustered more to the left of the mean with most of the extreme values to the right. A negative value indicates clustering to the right. Mathematically, skewness =

$$\frac{\sum_{i=1}^{N} [(X_i - \overline{X})/S]^3}{N}.$$

"Standard Error" helps to determine the potential degree of discrepancy between the sample mean and the usually unknown population mean. The standard error has properties very analogous to those of the standard deviations.

"Standard Deviation" measures the dispersion about the mean of an intervallevel variable. It measures the square root of the variance:

Standard Deviation =
$$\left[\frac{1}{N}\sum_{i=1}^{N}(X_i - \overline{X})^2\right]^{\frac{1}{2}}$$

The standard deviation is the positive square root of the variance and is another measure of variance. The standard deviation is, perhaps, the most important and most widely used measure of variability. A small volume of S denotes close clustering about the mean. A relatively large value represents wide scattering about the mean. The table shows relatively large values.

The range, maximum, and minimum present the usual extra data in the program. The statistical summary does not offer information adequately definitive to make conclusions required for the mission of this study. A Pearson's T test was performed with the SPSS package to establish any linear correlations among the various sets of data. A correlation of the various data sets was also performed with the IRM package in an attempt to further analyze the relationship between the various data sets.

The results of Pearson's correlation as performed with the SPSS are tabulated in Table 4. Output from this program included the correlation coefficient, the tests of significance, and the number of cases upon which the correlation coefficient was computed. Covariance, cross-product deviations for all combinations of pairs are shown in Table 5. In the graphical presentation of a typical set of data (Gravity, G, Figure 2), it appeared a priori unlikely to find a regression line, especially a straight one, which perfectly fits the data. Whether this is because the true relationship does not quite fit the curve being drawn or because of errors or imperfections in collecting the data, a measure of the goodness of fit of the regression line is desirable. The Pearson product moment correlation coefficient serves this purpose for linear regression. Where there is a fit (no error), it takes the value +1.0 or -1.0 where the sign is the same as the sign of the regression coefficient. A negative does not mean a bad fit; rather, it denotes an inverse relationship. When the linear-regression line is a poor fit to the data, it will be close to zero. The value of zero denotes the absence of a linear relationship.

If Pearson's coefficient is squared, we get another statistic which is a more easily interpreted measure of association when our concern is with the strength of relationship rather than with the direction of relationships. It varies from 0 to +10. (maximum). Its usefulness lies in the fact that the square of Pearson's coefficient is a measure of the proportion of variance in one variable explained by the other. A negative value for the correlation coefficient indicates a decrease in that property of the test with an increase in the compared property. Our test data in summary showed significant values of the correlation coefficients only for certain pairs (pp. 19 and 20).

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Table 4. Results of Pearson's Correlation as Performed Using the SPSS
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.5	300)	45.5.)	-	9415.	7,897	-	.3710	.587	٠.	72184	25	1664	1558	11.131	1234	626
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1	.2:34	1.1000		0111	93	-	2136	1551	2	•	00.30	.1271	.1248	197	1 4.4	. 22
	S= . J51		- 5	. 376.	5= .334	- ",	150.	691. 25	9 5 = .015	- ",	979 S	.261	(80) S= .927	2.5	136	(06)
1771	6418	111.	1	.334	9674.	•	1+53	19	.1820	4,00	1	1603	0 11110	200		
	- 17	_ ;	_ ;	5	(98)	- (809	000	_	_	801	800	809	72.00	1111.	7.00
	077	326.	-	100	1000	2=	.198	S= .0	=	= 0	816 S	595	\$= .692	7.7. =5	5= .320	S=
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	5=	5= .34		7	S =	- 5	100.	S=	_ 5	_ ",	901	801	100	1.4	100	000
,	::								,	;			N67. =6	S= .943	147. =5	368. =
****	3/16	2120	-	1453	*1**	1		119	•	3.	51	0676	0928	-17.27		23.50
	5= .131	55. =5	. "	136	100 = 5	- ",	100	S= 301	1 S= .779	_ ;	841	600	106	175	105	633
;									,	,		166.	214.	3= .576	625. =	\$01. =5
	.356.	1441.	٠.	1936	7643	:	.5119	1.6.5.	?	•	24	.1886	.1001	135		
		5= .169	. :	167	100	- ",			(98)	_ :	97)	800		(8))	979	33.
-			-					100	-	-	5 699	760.	S= .377	- St . 536	\$0 = C	S= .54
17.4	11.97	2718	•	1361	26800	•	6318	4858	1.	5200.	22	7540	3527	320	31.1	•
	J	2= 000	ر" -	100	199	_ ;	800	108	3	_		90	100	377	1 3.1	. LA
						,			1		304 2	189.	S= .580	S= . 334	5=	5= .234
CAAA	2189	3.		597	663	•	1910	45400	2200. *	1.0600	0.0	.7739	.0839	1.	2.1.2	
	5151	5= .973	- S	616	100	- 5	200	100	ز ـ	_ ;	3	106	(09)	175	1 3.1	1 831
						,		•			^ 10	101.	644. =5	3314	S=	S= .3.6
HAS	,cc1	1721.		0513	93	:	92900-	.1586	:	•	562	1.0000	.0339			
	3+1. =5	5= .261	- "	5 45		- 5	551	100 35	1 (80)	600		8	106	11.5	3.5	
,	135 1			1										5	5=1	5= .315
,	166)	1000	-	97)	108	•	8760.	1001.	1 0627	•	839	.0339	1.9900	+	.11.5	235
	3= .107	1200 = 5	. = 5	5 269.	.65.	S=	.413	S= .377	. "	- 15	. 654	201.	S= .301	100	175	176
a	.1 , 31	****	?.	1240	81		.4740	. 5 5 4	7 4238	0268	*	146	0,440			.020
			_	971 (200	_	301	831	-	-	1	809	AD	1.033		6:3.
	657. =5	5= .273		202	5+6.	"	.670	5= .036	=S	· = 5	14 5	904.	Se =2	S	S - 501	(re :
4,	1234	.15.6	1	1111	300	;	133	.2.86	:	.7107	20	. 3679	11125			
	42)	35	_ !		80)	_ ,	301	109	_	-) (6	900	106		*****	3
	212.	647.		326	167.	S=	.550	****	7	3:	31 5	.001	S= .320	- 5= . 11.	3: :	
a	*673*-	1425.		110	+960	•	0339		7.	7	,	4266	. 3205			
	\$67. =5	35 . 52	- "	. 155.	100	- :	100	331	833	833	3	30	106	1000		;
									;				366. =5	.Se		

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	VARIABLES	ò	CASES MEAN STD DEV	MEAN	STL	STD DEV			
				.1432	:	1.0003			
	¥210			2007		1.000			
	V100			007	: '	5666			
	73 - 1 A			8140	1.	1.6004			
	TEN		1 20	2000		1001			
-	C		90	6220	•	2 165			
	***		20	61.0.		1.1012			
	a a		-	1000.	•	9666.			
	. 3			10801	•	-6832			
	à		90	0000	• ::	1.0001			
VARL	VARIABLES	CASES	CROSS-PROD DEV	COVARIANCE		VARIABLES	CASES	CROSS-PROD DEV	COVARIANC
٠, د.	1,	36	17.5491	.2196	و	W210	6.0	-24.1748	
, ,		3 6	7464.03-	5898		VDEX	90	-29,3313	- 3713
	CRAM	0	-15.9053	7166.		***	00	-5.9046	0747
	5	90	-12.5108	1556	د. د	t 4 a	9 0	-15.1703	1667
	27.0	3 c	56.0.6-	1222		dd	90	-2.3272	160.
25		9 9	-16.891.8	0111	2	V100	98	-6.6400	-11094
4	TAN	9	-13.4120	-1548		100	9 9	12.2628	.1552
	H15 0	3 6	10.0561	.1273	1.4		2 0 0		7500.
1	56	30	3.4570	.0+38	1,5	3	00	14.2170	1001
121.	10c K	9 0	11.4017	.2203	v210	v100	10	41.8.1.	1624
¥21.0	TAN	90	8.9767	.1136	V210	CRAM	0 K	-15.0186	1961
127	O.A.	9 1	4.7573	. 4643	1211	0	90	-3.5496	2 420.
161.	44	• 0	-5.3512	2670	727	40	90	-8.6881	1100
1213	11	9.	-55.3272	7033	2357	YOUR	900	34.8787	. 4415
7.00	E KAR	9	4.6279	. 1611	42.0	SAH	000	1.5240	2550.
	. 3	2 2	-11.2711	1300	v 2 00	a	96	368	
Vuex	11	0	0 0 0 0 0 1	00000	3 4 6 7	4	90	-7.6123	1960
Verk	CRAM	90	1.1752	6410.	V DEX	14.0	0 4	0073.1	.0199
		0 :	-7.3340	9260	VOEX	a	200	-2.55.01	0677
	147	0 4	647.6-	742	*DEX	d	36	2.6806	250.
	141	800	14.6963	9250	> 7	CRAM	90	3.3058	.0418
	a	90	2.8970	. 1867	* >	0	38	7.9017	.1000
VI.	a	90	-5.4580	1507	T P N	OK BH	0 0	16.2637	.2059
TAN	a	20	-4.2504	0286	TAN	4	99	-3.0921	
TAN	aa	3 00	2,4016	0101	T A N	3	4.0	-10.2736	1300
CRAH	· ·	0 0	6.1057	1990	TAN D	SAH	80	56.1824	.7112
CKAH	73	9	51.6129	. 6533	144	4 4	300	-1.5315	6169
							10	-0.5476	1082

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CPOSS BROD WENT AND WORLD	ROD DEV COVARIANCE				-1.45770185
CASES CROSS P	1	90	80 -2.	80	80
VARIABLES		d a	44	4 °	400
COVARIANCE		2 0450		7020	.0114
CROSS-PROD DEV		67.9453	-2.4178	1.6153	.096.
CASES		9 9	08	90	78
VARIABLES	SAH	SAH CA	a.	99	99

Regression analyses were obtained to relate S & P, G & SAH, CRAM & N, CA & ZN, TBN & TAN, and V210 & V100 and to obtain equations for each pair. The correlation coefficient was obtained for each pair. These are shown in Table 4.

Pearson's correlation coefficient is used to measure the strength of relationship between two interval-level variables. In this case, the strength of relationship indicates both the goodness of fit of a linear regression line to the data and, when Pearson's coefficient is squared, the proportion of variance in one variable explained by the other.

Mathematically, Pearson's coefficient, r, is defined as the ratio of covariation to square root of the product of the variation in x and the variation in y where x and y symbolize the two variables. This corresponds to the formula:

$$r = \frac{\sum_{i=1}^{N} (X_{i} - \overline{X}) (Y_{i} - \overline{Y})}{\left\{ \left[\sum_{i=1}^{N} (X_{i} - \overline{X})^{2} \right] \left[\sum_{i=1}^{N} (Y_{i} - \overline{Y})^{2} \right] \right\}}$$

where:

 X_i = ith observation of variable x Y_i = ith observation of variable y

$$\overline{X} = \sum_{i=1}^{N} \frac{X_i}{N}$$
 = mean of variable x

$$\overline{Y} = \sum_{i=1}^{N} \frac{X_i}{N} = \text{mean of variable y}$$

The formula employed by SPSS for computing Pearson's coefficient is as follows:

Pearson's Correlation Coefficient
$$= \frac{\sum_{i=1}^{N} X_{i} Y_{i} - (\sum_{i=1}^{N} X_{i})(\sum_{i=1}^{N} Y_{i})/N}{\{ \left[\sum_{i=1}^{N} X_{i}^{2} - (\sum_{i=1}^{N} X_{i})^{2}/N \right] \left[\sum_{i=1}^{N} Y_{i}^{2} - (\sum_{i=1}^{N} Y_{i})^{2}/N \right] \}}$$

Significance tests are reported for each coefficient and are derived from the use of a student's T with N - 2 degrees of freedom for the computed quantity:

$$r\left[\frac{N-2}{1-r^2}\right]^{\frac{1}{2}}$$

where N = number of cases upon which the correlation coefficient was computed.

The tests of significance give information regarding the probability that the observed relationship could have happened by chance, i.e., probability that in a representative sample of a given size, the variables would exhibit a relationship as strong as the observed relationship. It has been accepted in other applications of SPSS to accept as statistically significant relationships which have a probability of occurrence by chance 5% of the time or less, i.e., in 5 out of 100 samples 0.05 or less. Applying this criteria, it can be noted that statistically significant results appear for the pairs listed below. A two-tailed list of significance as follows has been applied to the data:

Statistically significant	Pearson's correlation (absolute value)
G & FL	.2194
G & V ₂₁₀	.3059
G & V ₁₀₀	.5897
G & V EX	.3710
G & VÎ	.5874
G & TAN	.1197
G & CRAM	.2189
G & SAH	.1664
G & S	.1558
G & P	.1331
G & CA	.1284
FL & G	
FL & V ₁₀₀	.1093
FL & V EX	.2136
FL & VÎ	.1551
FL & TAN	.2718
FL & SAH	.1271
FL & CA	.1306
FL & pp	.2201
V ₂₁₀ & V ₁₀₀	.5296
$V_{210}^{210} \& V_{0}^{100} EX$.1453
$V_{210}^{210} \& V_{1}^{0}$.1900
V_{210}^{210} & TAN	.1820
V ₂₁₀ & SAH	.1271
V_{210}^{210} & CA	.1306
V ₂₁₀ & PP	.2201

	Pearson's correlation
Statistically Significant	(absolute value)
V ₁₀₀ & V _o EX	.4414
V ₁₀₀ & VI	.7703
V ₁₀₀ & TAN	.0802
V ₁₀₀ & CRAM	.0663
V ₁₀₀ & S	.1301
V ₁₀₀ & pp	.0964
V EX & VI	.5119
V _o EX & S	.0928
V EX & CA	.0730
VI & TAN	.0858
VI & SAH	.1886
VI & S	.1000
VI & P	.0537
VI & CA	.2080
VI & pp	.0691
TAN & CA	.2105
TAN & pp	.1346
TAN & S	.0627
CRAM & SAH	.7709
CRAM & S	.0839
CRAM & CA	.7167
CRAM & pp	.1174
SAH & P	.0941
SAH & CA	.8679
S & CA	.1125
CA & PP	.0530

Strong correlation relationships are shown between V_{210} and V_{100} (.5296), V_{100} and VI (.7703), V_o EX and VI (.5119), CRAM and SAH (.7709), CRAM and CA (.7167), and SAH and CA (.8679).

Because the correlation of a variable with itself is unity and the correlation of x with y is identical to the correlation of y with x, the redundant correlations are not included.

Factor Analysis

Factor analysis is a much more generalized procedure for evaluating and defining dimensional space among a relatively large number of variables. Because of the generality of factor analysis, it is difficult to present a capsule description of its functions and applications. The major use of factor analysis is to locate a small number of valid dimensions — clusters or factors contained in a larger set of independent items or variables. Factor analysis helps to determine the degree to which a given variable or several variables is part of a common, underlying phenomenon.

The single, most-distinctive characteristic of factor analysis is its data-reduction capability. From an array of correlation coefficients for a set of variables, factoranalysis techniques allow one to see whether some underlying pattern of relationships exists such that the data may be rearranged or reduced to a smaller set of factors or components that may be taken as source variables accounting for the observed interrelations in the data. In this study, one use of factor analysis was employed - explorthe exploration and detection of patterning of variables with a view toward the discovery of new concepts and a possible reduction of the data. Factor analysis is not a unitary concept. It subsumes a large number of procedures, the most general classification of which may be organized around major alternatives available at each of the customary steps. The steps are as follows: (1) the preparation of a correlation matrix, (2) the extraction of the initial factors - the exploration of possible data reduction, and (3) the notation to terminal solution the search for simple and interpretable factors. The factor matrix for the oil data is shown in Table 6. This application applies the scheme of correlation of variables (association) which in SPSS analysis is called R-factor analysis.

In general, there are many tests available for characterizing mineral oil lubricants, When engine tests, rig tests, and functional tests such as oxidation are omitted, many tests still remain. Some inspection tests, elemental analysis, and carbon-type analysis of lubricants are considered here. The object of the work again is to examine interrelationships to draw some inference about the significance of the tests in themselves and when taken in conjunction with others. This study is cognizant of both physical/chemical tests and separate engine tests but limits itself to selected chemical and physical tests in order to maintain some degree of simplicity in the interrelations. A subsequent study of the relationships will include other tests performed on engines. Many of the tests have been known for a long time and are considered to be standard in the industry.

The first step in factor analysis requires the calculation of a measure of association for relevant variables. The correlation matrix shown in Table 7 serves as the measure of association for the variables. The complete applications of the SPSS scheme to the analysis of these lubricating oils includes, in addition to the correlation matrix, a

	FACTOR 1	FACTOR 2	FACTOR 3	FACTOR 4	FACTOR 5	FACTOR 6	FACTOR 7	FACTOR 8	FACTOR 0	EACTOB
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	+ + 1 + 5 + 1 + 1	.17342	.26032	23212	02250	60000		. 36036	12724	.0274
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	4.73:1	******	116670	.02253	42837	76660		2	366396	*4410.
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	57606.	8476	- 24117		* ****	2070	01363	00347	-1246	1016
				****	.13584	26348	. 21514			161610
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TI WOTON	TACION 17	ACTOR 12 FACTOR 13	
. 31119		.01555	
16160		00464	
04372	•	1002.	
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1000		57,77	
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		7*010.	
. 46113	•	.26626	
. 10152	•	.62745	
00552	•	04023	
.21126		2057	
.04537	.64870	.10677	

COMMONALITY

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FL . 02739 V210 . 08635 V100 . 12145 V100 . 12145 V1 . 92134 V1 . 93514 CRAM . 08478		5	8
V210 V210 V210 V210 V210 V210 V210 V210			
	133	*8660**	52945
	555	. 15(33	.21997
	515	13412	65771
	241	07636	09631
	134	07532	.03399
	111	.23683	06911
	67.9	03678	.15152
	528	.67886	16596
	115	. 93188	12666
\$	135	.13663	.02052
1.60	:	14393	. 36347
14	. 313	1.00000	: 4966
80.	1.7	64966	1.06890

principal-component analysis. In principal-component analysis, the given set of variables is transformed by a transformation matrix into new sets of composite variables or components that are uncorrelated to each other. The transformation matrix is shown in Table 8. No particular assumption about the underlying structure of the variables is required or assumed. What is sought is the best linear combination of variables – best in the sense that the particular combination of variables would account for more of the variance in the data as a whole than any other combination of variables. The first principal component is then viewed as the single best summary of linear relationships exhibited in the data. The second component is viewed as the second best linear combination of variables under the condition that the second component is orthogonal to the first. To be orthogonal to the first component, the second must account for the portion of variance not accounted for by the first. Thus, the second component may be defined as the linear combination of variables that accounts for the most residual variance after the effect of the first component is removed from the data. Subsequent components are defined similarly until all the variance in the data is exhausted. Unless at least one variable is perfectly determined by the remainder of the variables in the data, the principal-component solution requires as many components as there are variables. The principal-component model may be compactly expressed as

$$Z_j = a_{j1} F_1 + a_{j2} F_2 + a_{j3} F_3 - a_{jn} F_n$$

where each of the n-observed variables is described linearly in terms of n new uncorrelated components F₁, F₂, F₃ ----- F_n, each of which is, in turn, defined as a linear combination of the n original variables. Since each component is defined as the best linear summary of variance left in the data after the previous components are taken care of, the first m components - usually much smaller than the number of variables in the set - may explain most of the variance in the data. For factor-analytic purposes, the analyst normally retains only the first few components for further rotation. The SPSS subprogram employed for these studies is known as principal factoring with iteration. The immediate result of the initial factoring was the extraction of an unrotated factor matrix shown in Table 6. The factors are arranged in the order of their importance. The first factor is the most important, the second factor is the second most important, etc. The first factor tends to be a general factor; it has significant loading on every variable. Subsequent factors tend to be bipolar, that is, some factor loadings are positive and some are negative. The method includes defined factors. The interest here is to find whether some smaller number of components accounts for most of the variance. From the unrotated factor matrix, it is obvious that factor 2(FL) has primary influence on factor CA, SAH, and CRAM and has negative influence on G. Factor 3(V210) has primary influence on TAN, FL, and P. Factor 4(V₁₀₀) has primary influence on pp and FL. Factor 5 (V₀EX) has primary influence on TAN, etc. Conversely, the influence of factor 2(FL) on VI and V EX is negligible.

Table 8. Transformation Matrix

FACTOR 1 .21136 .570441845035873 .0757418459 FACTOR 2 .9147404896 .99524 .09507 .1045915841	ACTOR 6 FACTOR 7	FACTOR 8	FACTOR 9	FACTOR 10
2 .9147404696 .09524 .09507 .10459		1		
10450.	•	61270.	37987.	. 43837
106.5		05792	.02110	21747
		- 774.11	14.862	45834
4 .0042314474 .06279 .33242		*****	26660	16091.
77.00		. 75093	.61109	00157
	•	.12878	04680	. 04435
. 14153 . 15706 16224 . 39605 . 77035	•	26585	17940	14476
7 .0375305460334438503 .31958		22920	20.70	0355
8 .04524 .4277314719 .4463.	1919	2000	901630	1996
D		.6663.	2.24/63	. 27177
11461.		38737	27554.	12019
- 11511. 1874516736 .1675	•	0.5042	95760	
11 . 18712 22004 69086 18787.				
10101	•	*****	15156	. 58959
Charles Charles Charles		62410.	.01652	24821
- 11380, -11004 1742 11004		7 7 7 7 7		

	FACTOR 11	FACTOR 12	FACTOR 13
ACTOR 1	-, 36,185	.06357	.51152
ACTOR 2	. 171.43	.26418	50176
ACTOR 3	.157.5	. 62186	97610
ACTOR 4	. 32241	06766	. 00003
ACTOR 5	. 30935	31740	06671
ACTOR 5	.07513	04191	.00436
ACTOR 7	-, 18815	62179	11315
ACTOR S	14135	61228	12828
ACTOR 9	01915	7806	. 01303
FACTOR 19	63335	.80173	05539
ACTOR 11	11645.	39904	19321
ACTOR 12	. 66231	. 33296	29577
ACTOR 13	. 32317	02527	93099
the same of the same of			

Table 9 shows the terminal solution of the orthogonally rotated data. It is an orthogonal-factor matrix and stands for both a pattern and a structure matrix. The coefficients in the table represent both the regression weights and the correlation coefficients. The loadings, or numbers, in a given row represent regression coefficients to describe a given variable. In the principal-component matrix, the eigenvalue (Table 10) associated with each component represents the amount of the total variance accounted for by the individual factor in the factor matrix (Table 6).

The total variance of a variable accounted for by the combination of all common factors is referred to as the communality of the variable. This value indicates the amount of the variance of a variable that is shared by at least one other variable in

the set. The proportion of total variance accounted for by a component is $\frac{\lambda_i}{n}$ where λ_i represents the eigenvalue of the ith component and n represents the number of variables in the set. From the data in Table 10, one sees that 85% of the total variance observed is accounted for by only 7 of the 13 pieces of analytical data about the lubricating oils. The number of significant components retained in the final rotation will be determined by the specification of the minimum eigenvalue criterion. The program retains and prints only components with eigenvalues greater than or equal to one. This criterion ensures that only components accounting for at least the amount of total variance of a single variable will be treated as significant.

Graphical representation of the notated data is shown in the illustrations that follow. SPSS in graphical representation allows the rotation of the factors one by one until every possible pair of factors has been plotted. Plotting the data in this fashion furnished information useful analytically in three ways: (1) the relative distance of the variable from the two axes, (2) the direction of the variable in relation to the axes and their relative positive or negative loading.), and (3) the clustering of the variables and their relative position to each other. Information relative to the degree of correlation is furnished from these observations. In the examples included, rotation of the factors has been accomplished by varimax rotation.

IV. DISCUSSION OF VARIMAX FACTOR MATRIX

From Table 6, it can be seen that the primary influence of G is by factor 1 with strong contributions by factors 2, 3, 6, 7, 8, 10, and 11. Other factors are negligible. For F1, the primary influence is by factor 4 with strong contributions by factors 1, 3, 6, 7, 8, and 9. Other factors are negligible. For V_{210} , the primary influence is by factor 1 with strong contributions by factors 2, 3, 5, 6, 7, and 8. Other factors are negligible. The other variables such as V_{100} . V_0 EX, VI, TAN, CRAM, SAH, S, P, CA, and pp are subject to the same analysis.

Table 9. Terminal Solution of the Orthogonally Rotated Data

	FACTOR 1	FACTOR 2	FACTOR 3	FACTOR 4	FACTOR 5	FACTOR 6	FACTOR 7	FACTOR 8	FACTOR 9	FACTOR 10
	13526	.34829	16893	16213	11915	.31718	16737	02034	.11347	.05528
	. 08 332	96136.	13696	.01255	90600.	01156	69355	.12558	.96914	76620.
7216	01739	67764	.18135	.97852	01926	.34371	. 0533	03847	16216.	19681
V100	30238	50945	.05788	.37263	08502	.18225	.21743	08470	16616	26765
VOEX	32991	23617	1887	.06063	04686	01961	.6656.	66420.	18424	12637
I	.14433	06976.	02411	06362	.05466	-, 11196	24355	04551	.05571	.25346
TAN	.01775	42981	.97424	.08326	01514	64240-	11675	.08892	13460	11516
CRAM	.71514	03993	.02904	.01573	.04380	10634	. 01823	06581	02670	06096
SAH	. 95+38	.06737	.34537	.07327	01821	. 14583	12893	.00057	.05411	05739
	.04023	.64658	61463	02181	.99228	14258	34212	. 01117	.03855	07356
	03523	01732	34454	.64413	04211	99566	11615	. 00513	01040	.00930
CA	.94238	.09162	33299	10605	.07323	10117	01925	02323	.06718	02745
99	03450	02472	09580	04076	.01138	.10535	. 1221.	.98628	.11676	01275

	FACTOR 11	FACTOR 12	FACTOR 13	
9	IZ355	03575	.00185	
F	00321	01101	.00003	
V210	.10759	69900.	00744	
V100	.57546	.00053	.00598	
VOEX	.06311	16790.	,5000.	
VI	12324	01861	.00271	
TAN	.02277	.01189	50304	
CRAM	.00932	.68903	00335	
SAH	03335	.06369	24431	
s	02336	.01658	.00339	
	. 12857	00232	90518	
CA	.03551	.61036	.26194	
99	03116	02520	76000-	

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CUM PCI PCT OF VAR EIGENVALUE Table 10. Principal Component Matrix FACTOR EST COMMONALITY 1.00000 1.00000 1.000000 1.000000 1.000000 1.00000 1.00000 1.00000 1.00000 VARIABLE VOIDE VOIDE

The values given in Table 6 represent regression coefficients of the factors to describe a given variable. For example, for the variable, G:

$$G = 0.72694F_1 - 0.39589F_2 + 0.22149F_3$$
$$-0.09300F_4 + 0.04745F_5 - 0.15405F_6$$
$$-0.10191F_7 + 0.19609F_8 + 0.07906F_9$$
$$+ 0.26917F_{10} + 0.31050F_{11} - 0.08497F_{12}$$
$$+ 0.01619F_{13} .$$

where F_1 = factor 1, etc. The other variables such as FL, V_{210} , and V_{100} would be treated in a similar manner.

The general equation

$$Z_{j} = a_{j1}F_{1} + a_{j2}F_{2} + \cdots + a_{jm}F_{m} + d_{j}U_{j}$$

expresses this relationship.

The variance accounted for by factor 1 is

$$(a_{11})^2 = (0.72694)^2 = 0.5284$$

The variance accounted for by factor 2 is

$$(a_{12})^2 = (0.39589)^2 = 0.1567,$$

etc.

$$\sum_{j=1}^{N} a_{j1}^{2} \quad j = 1, 2, 3, ..., N$$

$$= (.72694)^{2} + (.34124)^{2} + + (.01003)^{2} = 2.98602$$

$$= \text{respective eigenvalue}.$$

These values are shown in Table 6 along with cumulative percentages in Table 10.

Significantly, most of the variance in the data is accounted for by G and FL. The unrotated factors extracted through the factoring method may or may not give meaningful patterning of the variables. To supplant the data obtained from the unrotated factors, the factors are subsequently rotated to effect additional simplication.

Rotation in Subprogram

In this SPSS program, all the initial solutions extract orthogonal factors in order of their importance. The first factor so extracted tends to be a general factor; that is, it tends to load significantly on every variable. The second factor tends to be bipolar, that is, approximately half the variables have positive loadings and the other half have negative loading. The remaining factors also tend to be bipolar, and it is difficult to interpret such factors. Every variable tends to be decomposed into both positive and negative factors, and the complexity of each variable is usually greater than one.

The analytical method of rotation is designed to take a fixed number of factors and a fixed amount of variance accounted for by these factors and simplify the rows of the factor matrix and the column matrix to make as many values as possible in each row and column close to zero.

In the illustrations that follow, the SPSS depicts graphical presentation of rotated orthogonal factors employing a procedure termed varimax. Varimax centers on simplifying the columns of the factor matrix. A simple factor is defined in varimax as one with only 1s and 0s in the column. This simplification is equivalent to maximizing the variance of the squared loadings in each column. Since only two-dimensional space can be effectively plotted, every possible pair of factors is taken one by one. Significance of the graphs resides in three aspects: (1) the relative distance of a variable from the two axes, (2) the direction of a variable in relation to the axis (It may indicate either a positive or negative loading.), and (3) the clustering of variables and their relative position to each other. Conclusions relative to the degree of actual correlation between the factors are drawn from these observations.

In Figure 3, variables 2, 3, 5, 7, 10, and 13 load low on factor 2. Variables 8, 9, and 12 load high on factor 1, and variable 6 loads low on factor 1 and high on factor 2. In addition, variables 10, 2, 13, 7, 3, and 5 are close to the origin and have small loadings on both factor 1 and factor 2. As a whole, the graph separates cluster 10, 2, 13, 7, 3, and 5 from cluster 8, 9, and 12. The clustering of these groups indicates some degree of correlation between them. Variable 11 did not load significantly on either axis.

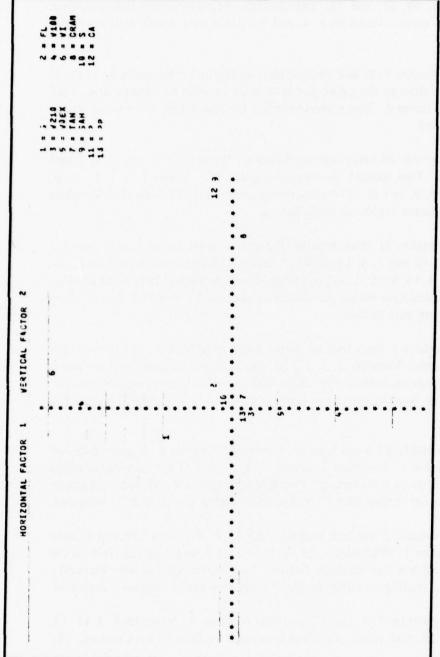


Figure 3. Horizontal Factor 1; Vertical Factor 2.

In Figure 4, variables 8, 9, and 12 load high on factor 1 and cluster. Variables 1, 2, 6, 10, 11, and 13 are all close to the origin and have small loadings on both factors. Variable 7 loads high on factor 3. The graph separates cluster 8, 9, and 12 from cluster 1, 2, 6, 10, 11, and 13. The clustering of these groups indicates some correlation between them. Variables 3, 4, and 5 did not load significantly on either axis.

In Figure 5, variables 8, 9, and 12 load high on factor 1. Variables 5, 7, 11, 2, 13, 10, 6, and 1 are close to the origin and have small loadings on both factors. Variable 3 loads high on factor 4. Two separate clusters are observable. Correlation within the clusters is indicated.

In Figure 6, variable 10 loads high on factor 5. Variables 2, 6, 13, 1, 4, 7, and 11 show clustering. Two distinct clusters are observable — cluster 1, 4, 7, 11, 2, 6, and 13 and cluster 8, 9, and 12. Correlation within the clusters is indicated. Variables 3 and 5 show insignificant loading on both factors.

In Figure 7, variable 11 loads high on factor 6, low on factor 1 and clustering occurs for 8, 9, and 12 and 1, 4, 13, 5, 10, 2, and 6. Two distinct clusters are observable. Variables 1, 4, 13, 5, 10, 2, and 6 are close to the origin and have small loadings on both factors. Correlation within the clusters is indicated. Variables 3 and 7 show insignificant loading on both factors.

In Figure 8, variable 5 loads high on factor 7 and variables 8, 9, and 12 load high on factor 1 and cluster. Variables 1, 2, 11, 10, 13, 3, 4, and 6 cluster near the origin and have small loadings on both factors. Two distinct, separate groups are observable. Variable 7 shows no loading on either factor. Correlation is indicated within the clusters.

In Figure 9, variable 13 loads high on factor 8. Variables 8, 9, and 12 cluster and load high on factor 1. Variables 1, 3, 4, 6, 2, 7, 10, and 11 are close to the origin and have small loadings on both factors. Two distinct groups are observable. Variable 5 shows no loading on either factor. Correlation within the clusters is indicated.

In Figure 10, variable 2 has high loading on factor 9. Variables 8, 9, and 12 have high loadings on factor 1. Variables 1, 13, 3, 10, 6, 11, 5, and 7 are all close to the origin and have small loadings on both factors. Two distinct groups are observable. Variable 4 shows no loading on either factor. Correlation within clusters is indicated.

In Figure 11, variables 8, 9, and 12 load high on factor 1. Variables 6, 2, 11, 13, 10, 5, 7, and 4 are all close to the origin and have small loadings on both factors. The

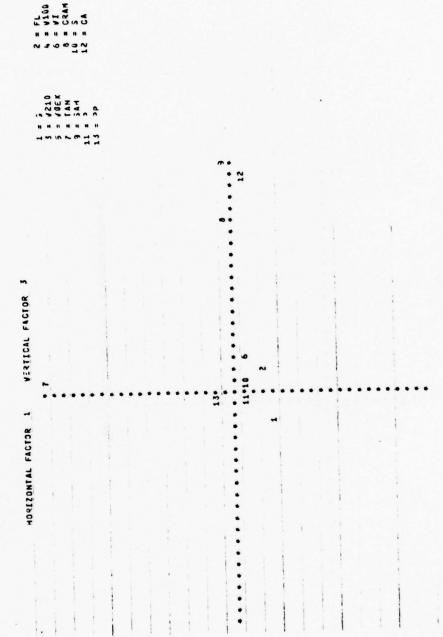
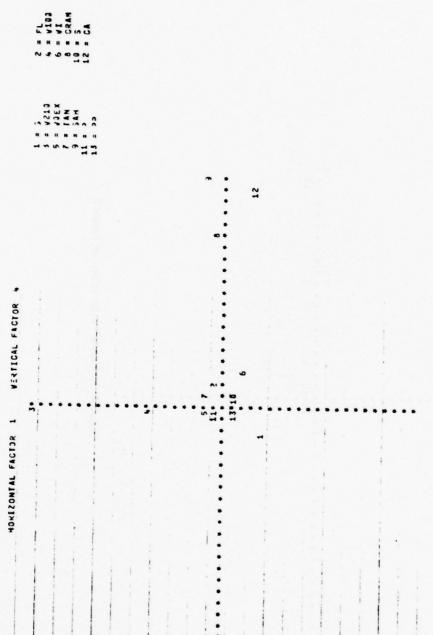


Figure 4. Horizontal Factor 1; Vertical Factor 3.



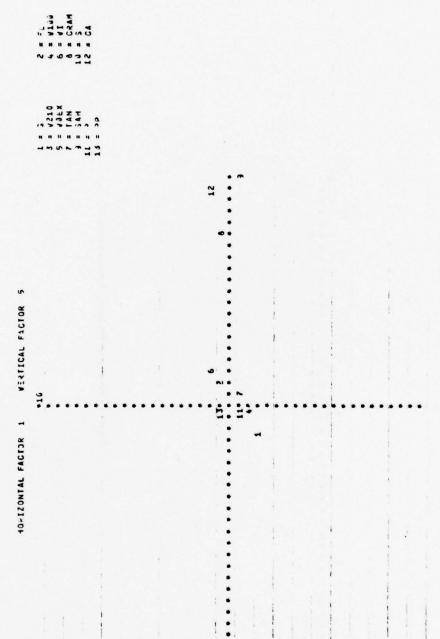


Figure 6. Horizontal Factor 1; Vertical Factor 5.

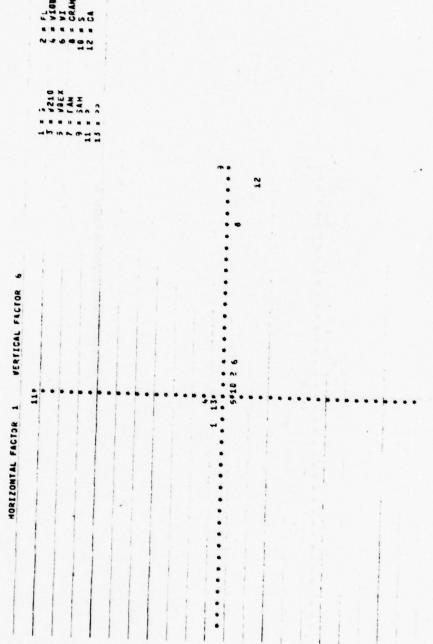


Figure 7. Horizontal Factor 1; Vertical Factor 6.

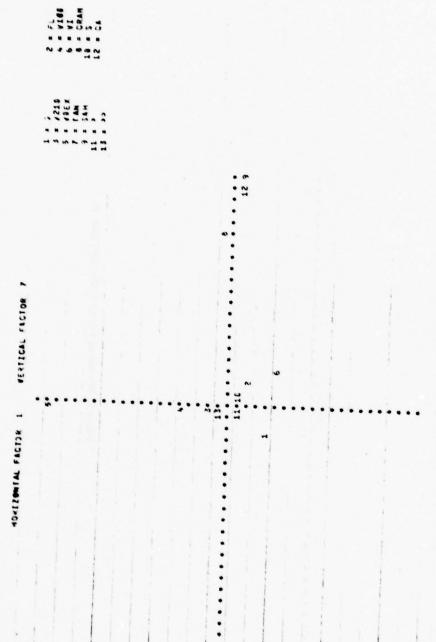


Figure 8. Horizontal Factor 1; Vertical Factor 7.

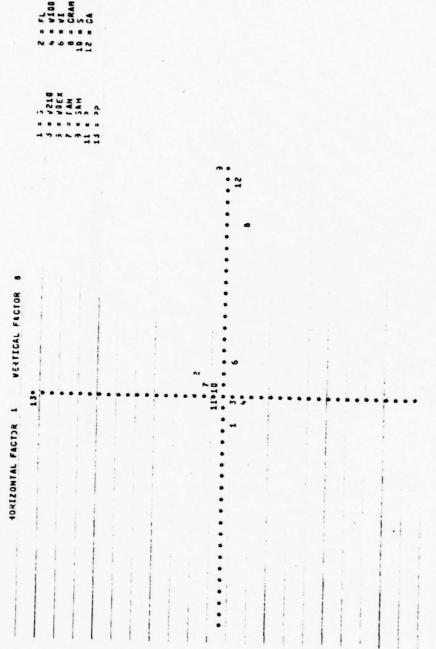


Figure 9. Horizontal Factor 1; Vertical Factor 8.

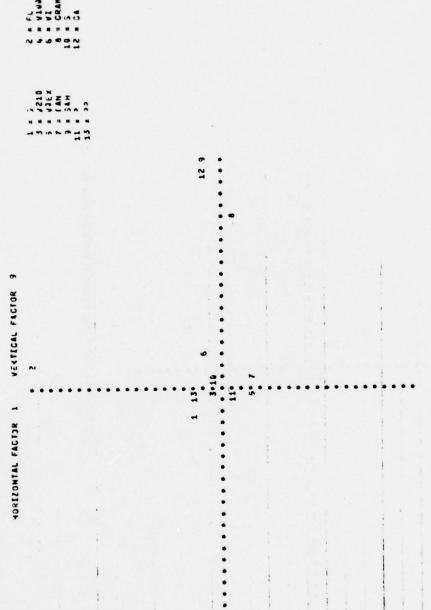


Figure 10. Horizontal Factor 1; Vertical Factor 9.

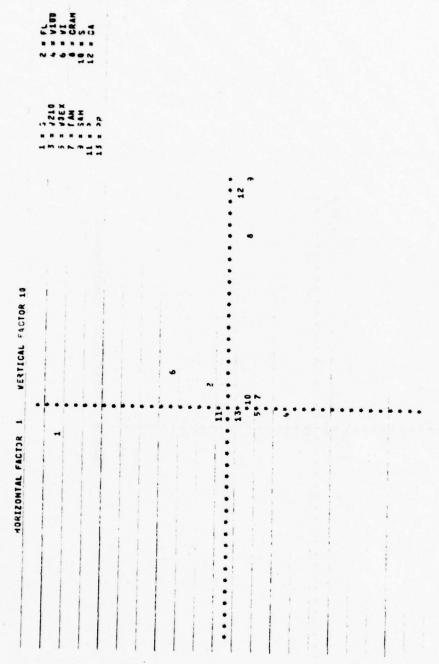


Figure 11. Horizontal Factor 1; Vertical Factor 10.

clusters of variables 8, 9, and 12 and 6, 2, 11, 13, 10, 5, and 7 separate the variables into two groups. Correlation within the two groups is indicated. Variable 3 shows no significant loading on either factor.

In Figure 12, variable 4 loads moderately high on factor 11. Variables 1, 6, 13, 10, 2, 11, 7, 5, and 3 are all close to the origin and have small loadings on both factors. Variables 8, 9, and 12 load high on factor 1 and have small loadings on factor 11. Two separate clusters are indicated with correlation within the clusters.

In Figure 13, variables, 1, 13, 2, 6, 5, and 10 all are close to the origin and have small loadings on both factors. Variables 9 and 12 have high loadings on factor 1. Variable 8 has significant loading on both factor 12 and factor 1. Variables 3, 4, 7, and 11 have no significant loading on either factor. Correlation within the clusters is indicated.

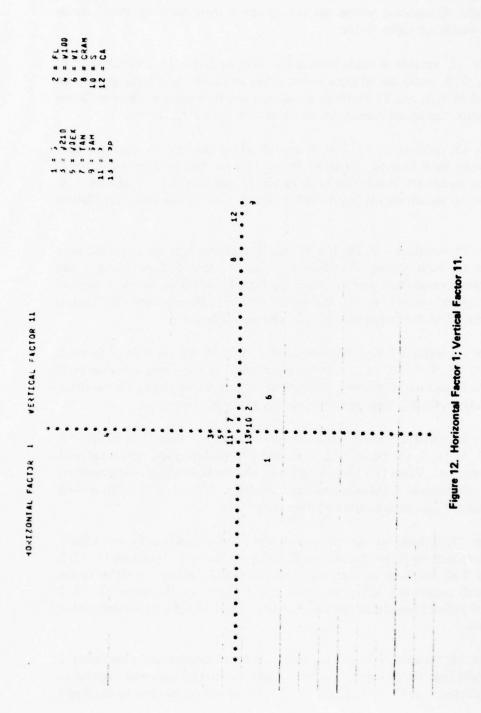
In Figure 14, variables 1, 5, 10, 2, 6, 13, and 7 all cluster near the origin and have small loadings on both factors. Variables 8, 9, and 12 load high on factor 1 and cluster less close; variables 9 and 12 show significant loading on factor 1 and are negative. Two groups are observable. Variables 3, 4, and 11 show insignificant loading on either factor. Correlation between the two groups is indicated.

In Figure 15, variable 7 loads high on factor 3. Variable 6 loads high on factor 2. Variables 5, 3, 13, 8, 9, 10, 11, 12, and 2 are all close to the origin and have small loadings on both factors. Clustering is indicative of correlation among the variables. Variable 4 loads moderately high on factor 2 and is negatively correlated.

In Figure 16, variable 3 loads high on factor 4. Variable 6 loads high on factor 2. Variables 5, 7, 9, 11, 2, 13, 10, and 12 all are close to the origin and have small loadings on both factors. Variable 4 loads moderately high on both factors and negatively on factor 4. Correlation is indicated within variables 5, 7, 9, 11, 2, 13, 10, and 12. Variable 8 does not load significantly on either factor.

In Figure 17, variable 10 loads high on factor 5 and insignificantly on factor 2. Variable 6 loads high on factor 2 and insignificantly on factor 5. Variables 13, 12, 2, 5, 3, 11, and 9 all are close to the origin and have small loadings on either factor. Variable 4 loads moderately heavy on factor 2 and negatively. Variables 12, 13, 2, 5, 3, 11, and 9 indicate correlation within. Variables 7 and 8 have insignificant loading on both factors.

In Figure 18, variable 11 loads high on factor 6 and insignificantly on factor 2. Variable 6 loads high on factor 2. Variable 4 loads moderately high and negative on factor 2. Variables 3, 2, 13, 9, 5, 8, 10, and 12 cluster and are all close to the origin.



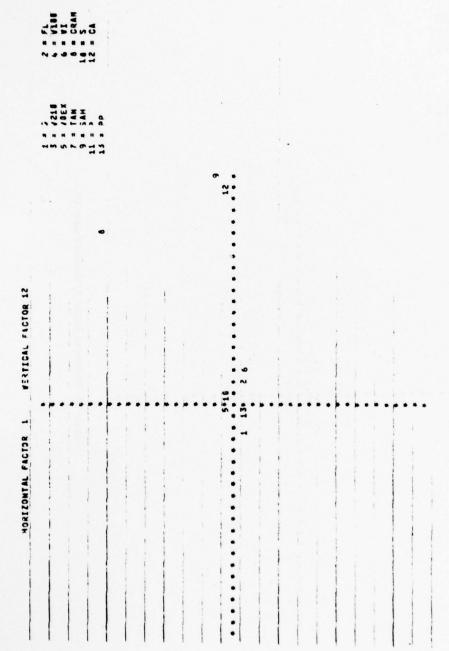


Figure 13. Horizontal Factor 1; Vertical Factor 12.

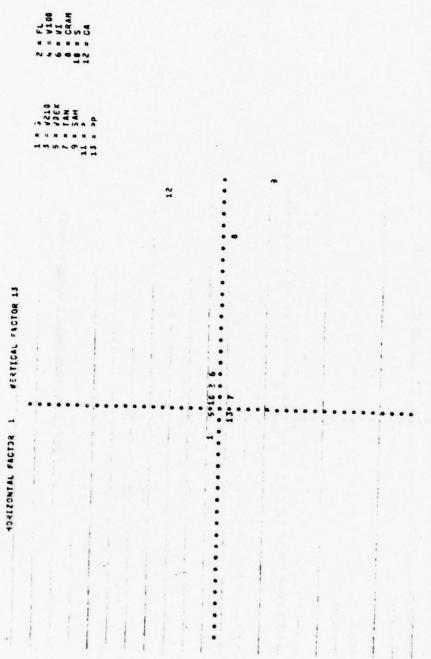


Figure 14. Horizontal Factor 1; Vertical Factor 13.

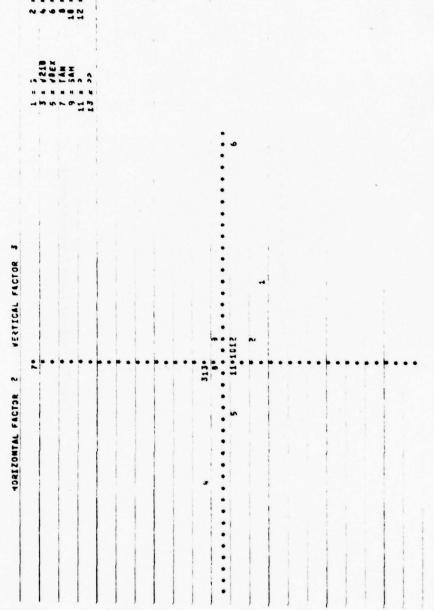
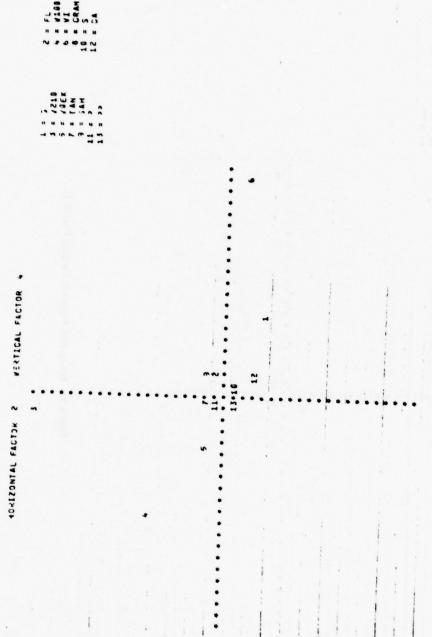


Figure 15. Horizontal Factor 2; Vertical Factor 3.



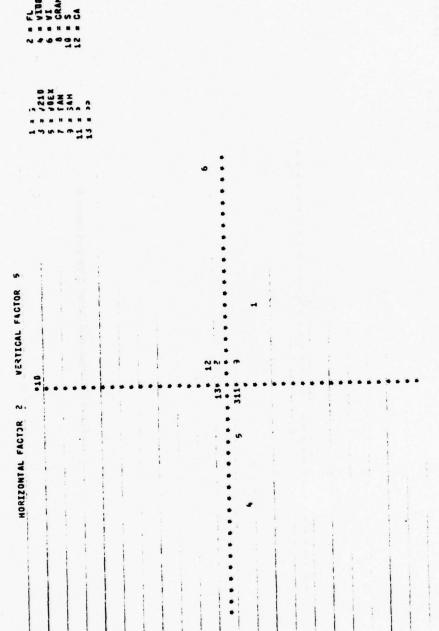


Figure 17. Horizontal Factor 2; Vertical Factor 5.

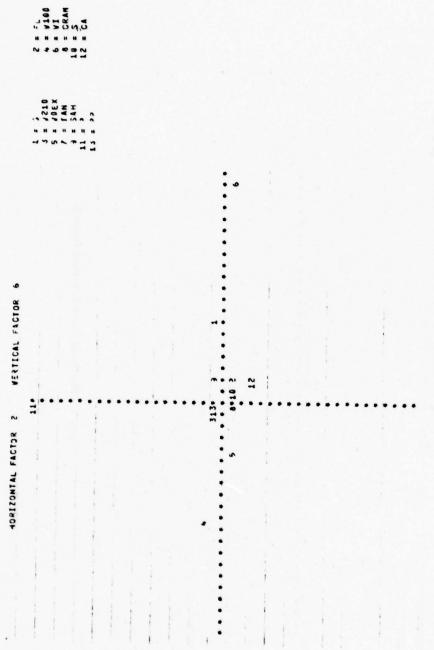


Figure 18. Horizontal Factor 2; Vertical Factor 6.

They have small loadings on both factors and indicate some internal correlation. Variable 7 loads insignificantly on both factors.

In Figure 19, variables 5 and 6 load high (negatively) on factors 7 and 2 respectively. Variables 4 and 1 load negatively and moderately on factors 2 and 7 respectively. Variables 3, 13, 10, 11, 12, and 2 cluster and are close to the origin with small loadings on each factor. Variables 3, 13, 10, 11, 12, and 2 correlate.

In Figure 20, variable 13 loads high on factor 8. Variable 6 loads high on factor 2. Variables 2, 7, 5, 9, 10, 11, 3, 8, 12, and 1 cluster and are close to the origin. Also, they all have small loadings on both factors. Variable 4 loads negatively and moderately high on factor 2.

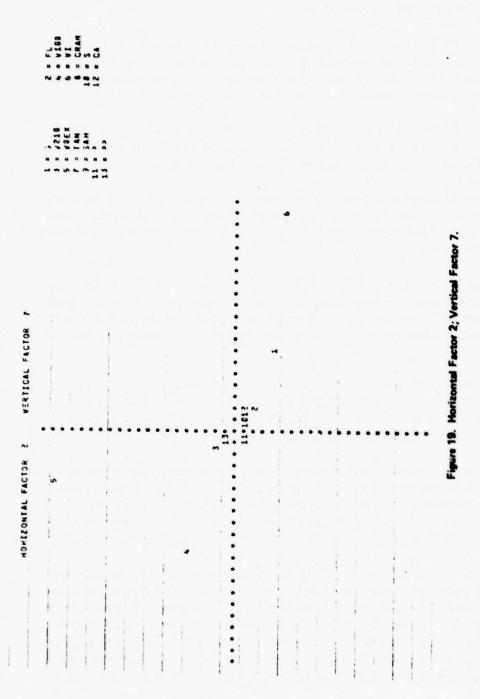
In Figure 21, variable 6 loads high on factor 2. Variable 2 loads high on factor 9. Variables 3, 5, 7, 10, 11, 12, and 13 cluster and are close to the origin. Small loadings on both factors and correlation are indicated. Variables 8 and 9 load insignificantly on both factors.

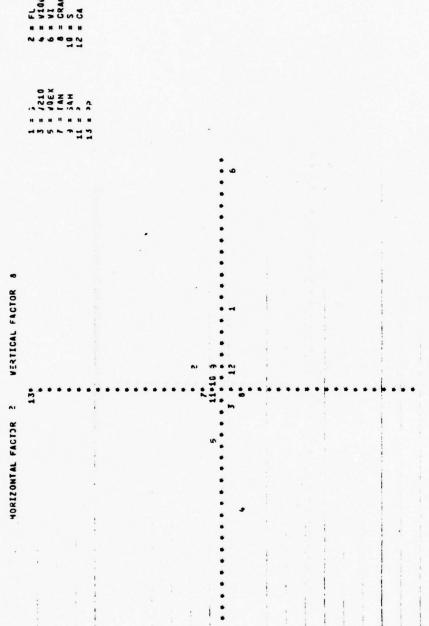
In Figure 22, variables 2, 3, 5, 7, 8, 9, 10, 11, 12, and 13 are close to the origin and have small loadings on both factors. Correlation is indicated. Variable 1 loads high on factor 10. Variable 6 loads high on factor 2. Both variables 1 and 6 load on factors 10 and 2 respectively. Variable 4 loads negatively and moderately high on factor 2.

In Figure 23, variables 5, 3, 11, 12, 10, 13, and 9 cluster, are near the origin, and have small loadings on both factors. A degree of correlation is indicated. Variable 6 loads high on factor 2. Variable 4 loads moderately high on factors 2 and 11. Variable 2, 7, and 8 show insignificant loadings on both factors.

In Figure 24, variable 6 loads high on factor 2 and insignificantly on factor 12. Variable 8 loads high on factor 12. Variables 5, 3, 7, 9, 10, 12, 13, and 2 cluster, are close to the origin, and have small loadings on both factors. Correlation is indicated. Variable 11 exhibits insignificant loading on both factors. Variables 4, 5, and 1 load moderately high on factor 2 with variables 4 and 5 having a negative correlation.

In Figure 25, variables 3, 13, 2, 10, and 5 cluster and are close to the origin. There is no significant loading on either factor. The degree of cluster formation lessened. Correlation is indicated for variables 3, 2, 13, 10, and 5. Variable 6 loads high on factor 2. Variables 4, 3, 5, 10, 2, 1, and 6 have insignificant loading on factor 13. Variables 4 and 5 have a negative correlation. Variables 2, 7, and 8 show insignificant loading on either factor. Correlation as it relates to factor 2 and factor 13 is more limited. Variables 9 and 12 load on factor 13 with variable 9 having a negative correlation.





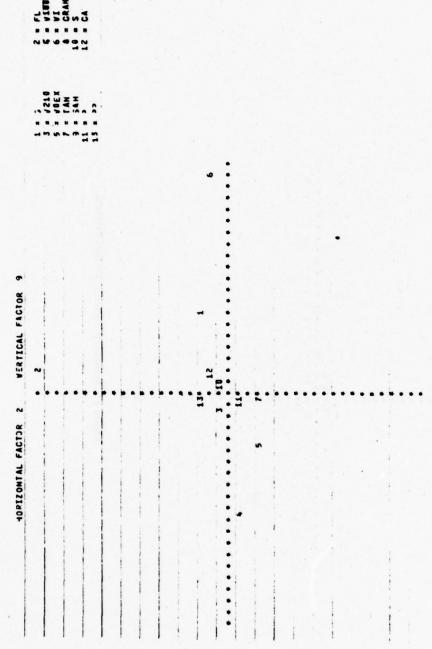
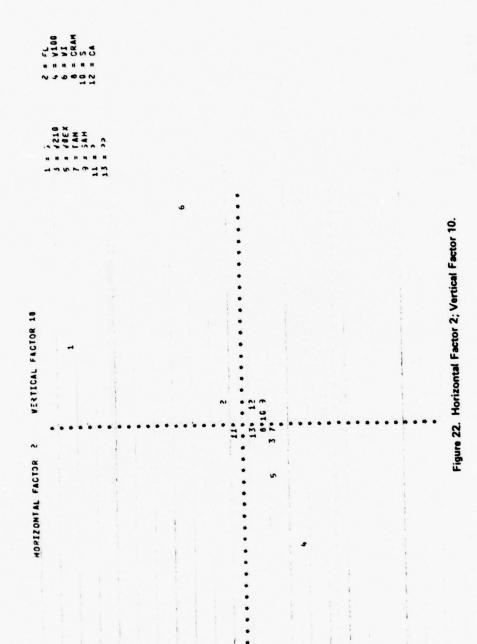


Figure 21. Horizontal Factor 2; Vertical Factor 9.



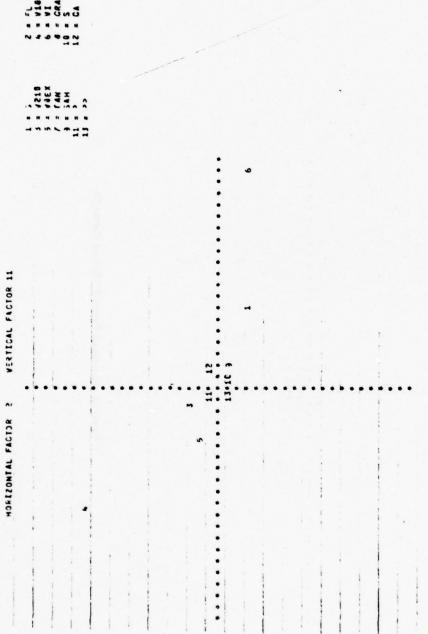


Figure 23. Horizontal Factor 2; Vertical Factor 11.



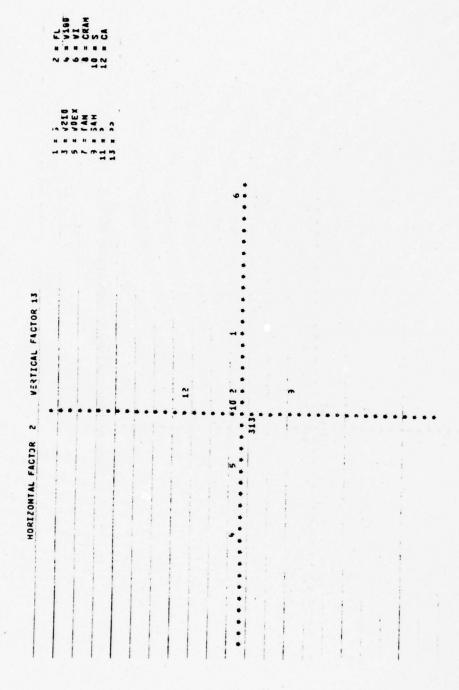


Figure 25. Horizontel Factor 2; Vertical Factor 13.

In Figure 26, variables 2, 5, 9, 11, 8, 10, 13, 6, and 12 cluster and are close to the origin. Group correlation is indicated. Variable 7 loads high on factor 3. Variable 3 loads high and variable 4 loads moderately on factor 4.

In Figure 27, variables 1, 2, 3, 4, 8, 9, 11, 12, and 13 cluster and are close to the origin. Small loadings on either factor and correlation are indicated. Variable 7 loads high on factor 3. Variable 10 loads high on factor 5. Only one grouping of variables is indicated. Variables 5 and 6 have insignificant loading on both factors.

In Figure 28, variables 1, 4, 9, 13, 2, 10, 8, and 12 cluster and are close to the origin. Small loading exists on either factor. Correlation is indicated. Variable 11 loads high on factor 6. Variable 7 loads high on factor 3. Variables 5, 3, and 6 show no loading.

In Figure 29, variables 4, 3, 8, 13, 12, 9, 2, 1, and 6 cluster and are close to the origin. Small loading exists on either factor. Correlation is indicated. Variable 5 loads high on factor 7. Variable 7 loads high on factor 3. Variables 10 and 11 show no significant loading on factor 3 or factor 7 respectively.

In Figure 30, variables 2, 9, 11, 1, 12, 3, 8, and 4 cluster and are close to the origin. Small loading exists for either factor. Correlation is indicated. One main grouping exists. Variable 7 loads high on factor 3. Variable 13 loads high on factor 8 — one group of the data indicated. Variables 5, 6, and 10 show no loading on either factor.

In Figure 31, variables 4, 8, 11, 5, 3, 10, 12, 9, 1, and 13 are clustered. All are near the origin and have small loadings on either factor. Internal correlation is indicated. Variable 2 loads high on factor 9. Variable 7 loads high on factor 3. Variable 6 shows no loading on either factor.

In Figure 32, variables 2, 6, 11, 12, 13, 10, 9, 5, and 3 cluster and all are close to the origin. Internal correlation is indicated. Variable 7 loads high on factor 3. Variable 1 loads high on factor 10. Variable 8 shows no loading of significance.

In Figure 33, variables 3, 5, 12, 8, 2, 10, 9, 13, 1, and 6 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 7 loads high on factor 3. Variable 4 loads high on factor 11. One group of variables is indicated. Variable 11 shows no loading on either factor.

In Figure 34, variables 4, 9, 12, 1, 2, 11, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 7 loads high on factor 3. Variables 3, 5, 6, and 10 have no significant loading on either factor. Variable 8 loads high on factor 12.

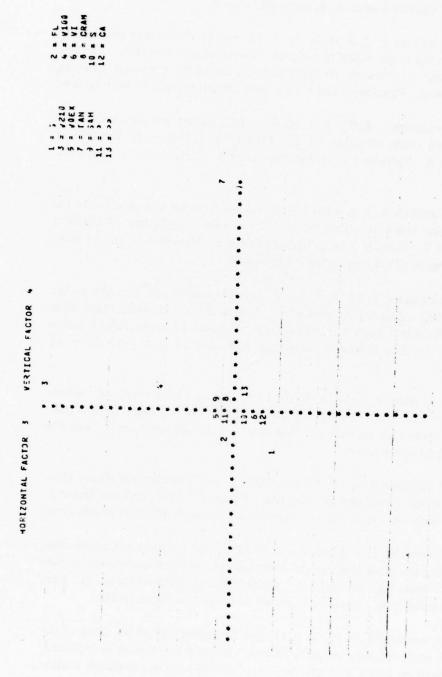


Figure 26. Horizontal Factor 3; Vertical Factor 4.

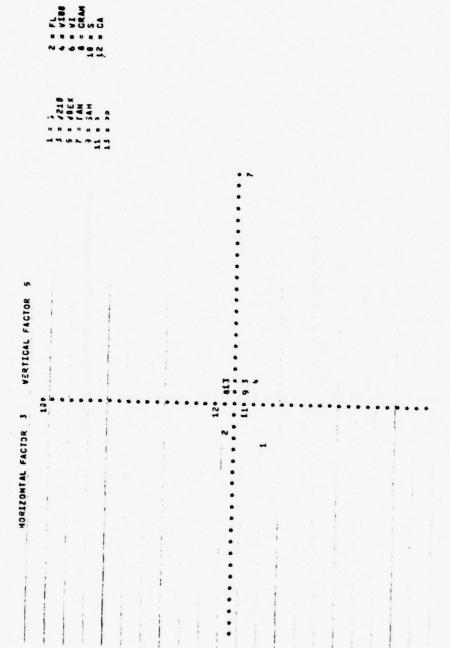


Figure 27. Horizontal Factor 3; Vertical Factor 5.

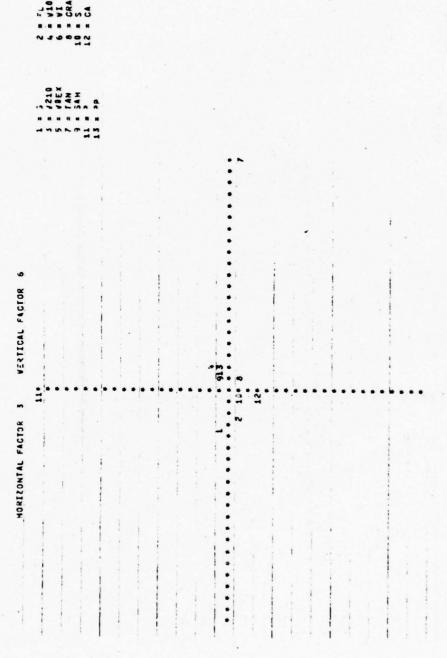


Figure 28. Horizontal Factor 3; Vertical Factor 6.

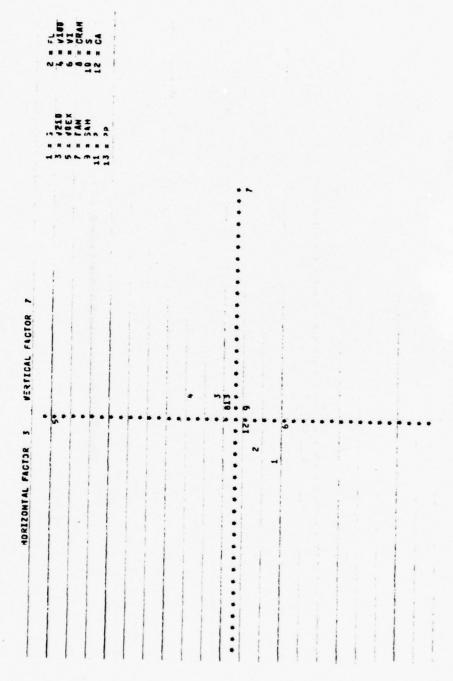


Figure 29. Horizontal Factor 3; Vertical Factor 7.

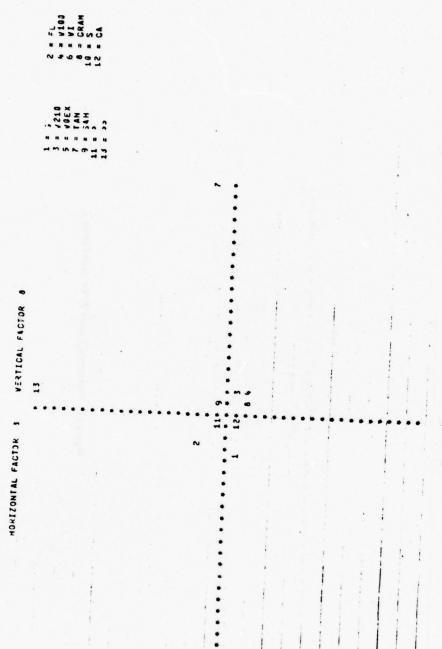


Figure 30. Horizontal Factor 3; Vertical Factor 8.

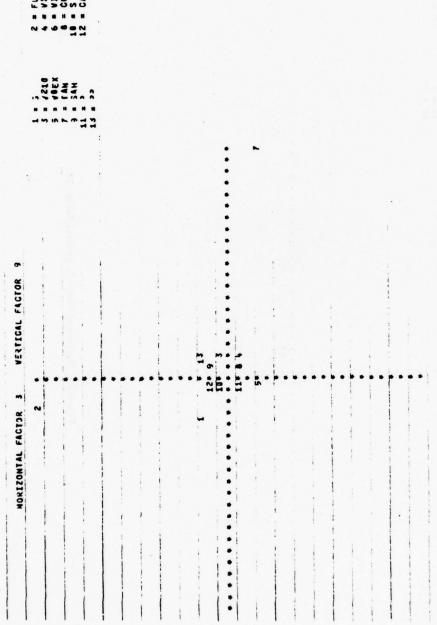


Figure 31. Horizontal Factor 3; Vertical Factor 9.

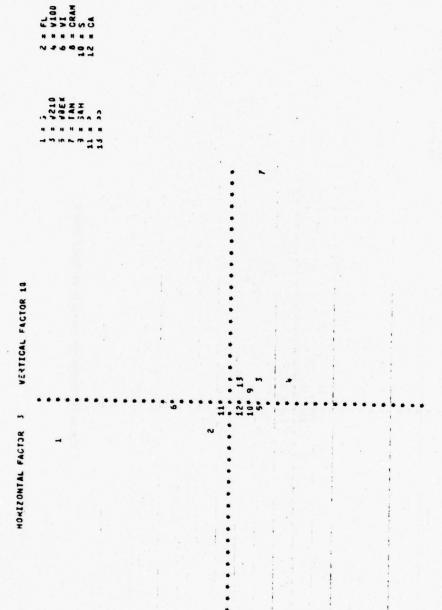


Figure 32. Horizontal Factor 3; Vertical Factor 10.

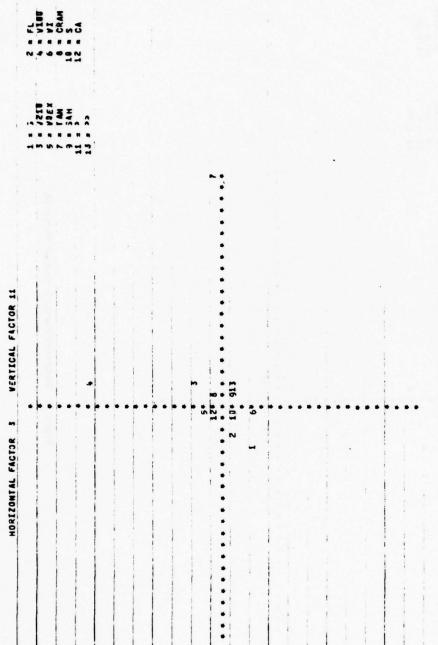


Figure 33. Horizontal Factor 3; Vertical Factor 11.

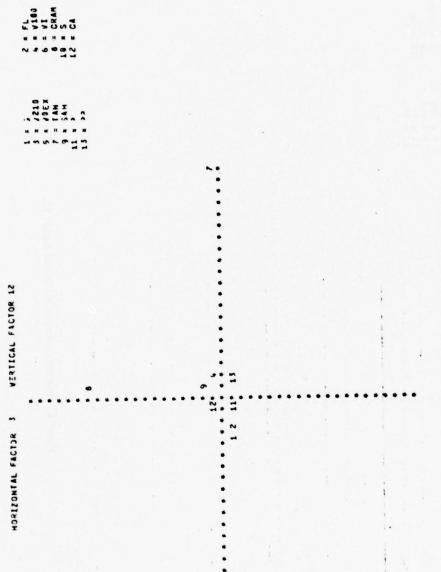


Figure 34. Horizontal Factor 3; Vertical Factor 12.

In Figure 35, variables 1, 2, 10, 4, 12, 11, 8, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 7 loads high on factor 3. Variables 3, 5, and 6 show insignificant loadings on both factors.

In Figure 36, variables 12, 6, 13, 8, 11, and 9 cluster and are all close to the origin All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4; variable 10 loads high on factor 5. Variables 2, 5, and 7 do not load significantly on either factor.

In Figure 37, variables 1, 13, 9, 6, 10, 8, 7, and 12 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4; variable 6 loads high on factor 4. Variables 2 and 5 show no significant loading on either factor.

In Figure 38, variables 13, 8, 12, 10, 11, 9, and 2 cluster and are all close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4; variable 5 loads high on factor 7. Variable 7 shows insignificant loading on both factors.

In Figure 39, variables 2, 7, 10, 11, 9, 1, 12, 6, and 8 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4. Variable 13 loads high on factor 8. Variable 5 shows insignificant loading on both factors.

In Figure 40, variables 1, 13, 12, 6, 10, 9, and 11 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4; variable 2 loads high on factor 9. Variables 5 and 8 show insignificant loading on either factor.

In Figure 41, variables 2, 11, 12, 13, 10, 8, 9, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4. Variable 1 loads high on factor 10. Variable 5 shows insignificant loading on either factor.

In Figure 42, variables 5, 7, 11, 12, 2, 9, 13, 1, and 6 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4. Variable 4 loads moderately high on both factors. Variable 10 shows insignificant loading on either factor.

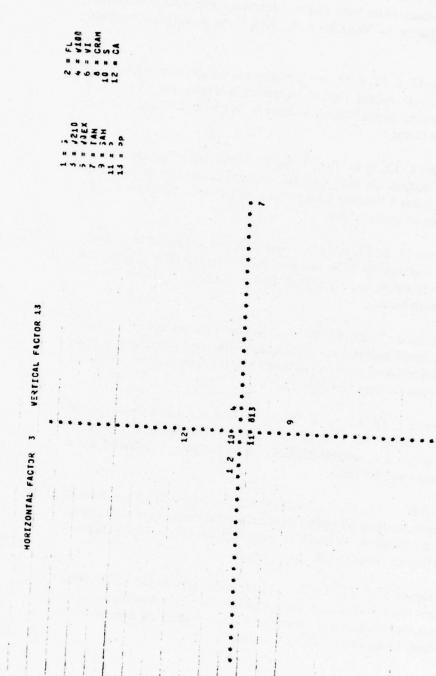
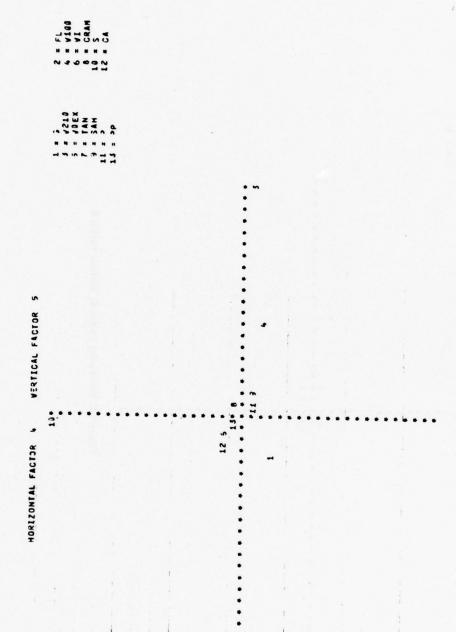
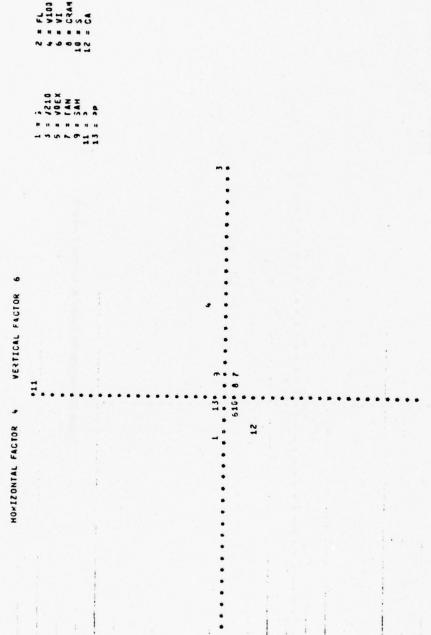
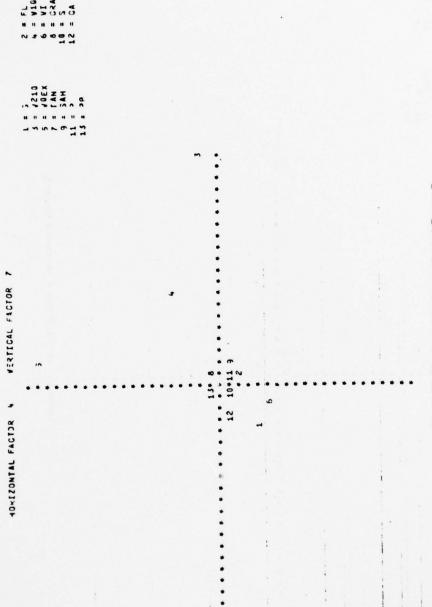


Figure 35. Horizontal Factor 3; Vertical Factor 13.







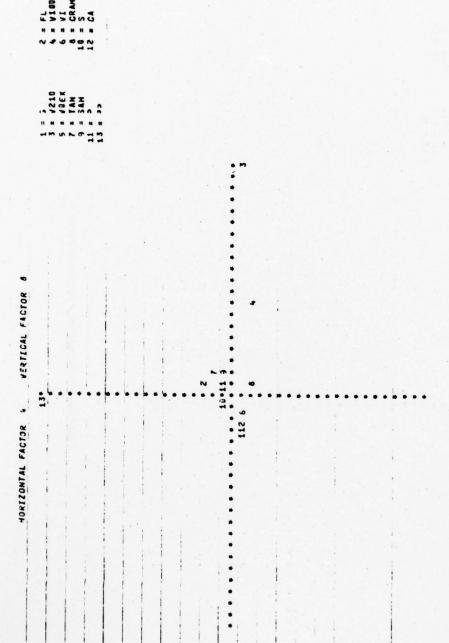


Figure 39. Vertical Factor 4; Horizental Factor 8.

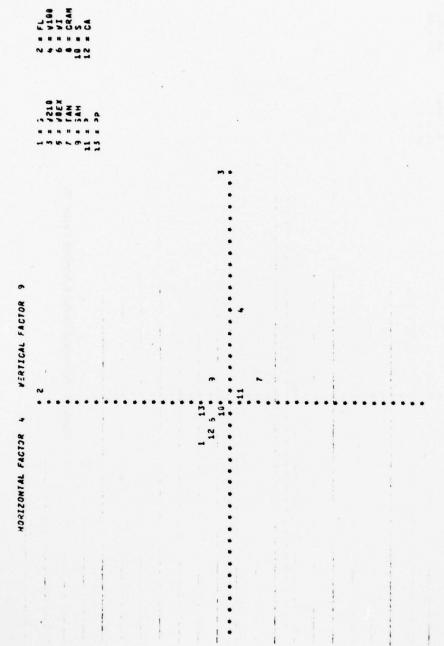
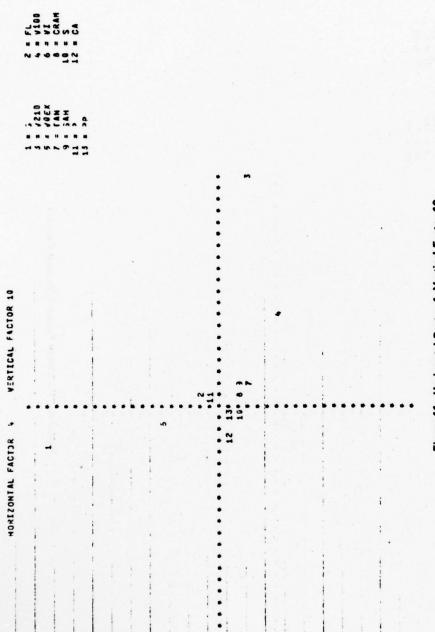
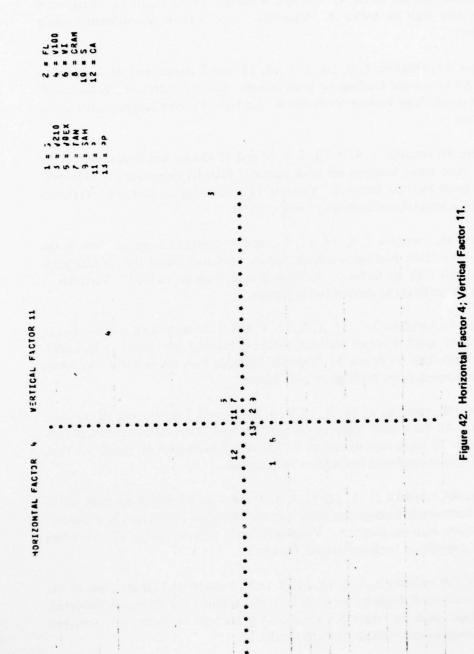


Figure 40. Horizontal Factor 4; Vertical Factor 9.





In Figure 43, variables 9, 10, 11, 12, 13, 1, 6, and 7 cluster and are all close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 loads high on factor 4. Variable 8 loads high on factor 12. Variable 4 loads moderately high on factor 4. Variables 2 and 5 show insignificant loading on both factors.

In Figure 44, variables 1, 6, 10, 2, 5, 13, 11, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 3 exhibits high loading on factor 4. Variable 8 shows insignificant loading on either factor.

In Figure 45, variables 1, 4, 9, 13, 7, 8, 6, and 12 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 11 loads high on factor 6. Variables 2, 3, and 5 show insignificant loadings on either factor.

In Figure 46, variables 4, 3, 13, 11, 12, and 1 cluster and are all close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 5 loads high on factor 7. Variables 7, 8, and 9 have insignificant loadings on both factors.

In Figure 47, variables 2, 7, 11, 1, 3, 12, 4, and 8 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 13 loads high on factor 8. Variables 5, 6, and 7 have insignificant loadings on both factors.

In Figure 48, variables 1, 13, 9, 12, 3, 4, 11, 8, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 2 loads high on factor 9. Variables 5 and 6 have insignificant loadings on both factors.

In Figure 49, variables 2, 11, 12, 13, 7, 8, 9, and 4 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 1 loads high on factor 10. Variables 5 and 3 have insignificant loadings on both factors.

In Figure 50, variables 3, 5, 8, 12, 11, 9, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 4 loads high on factor 11. Variables 2 and 7 have insignificant loadings on both factors.

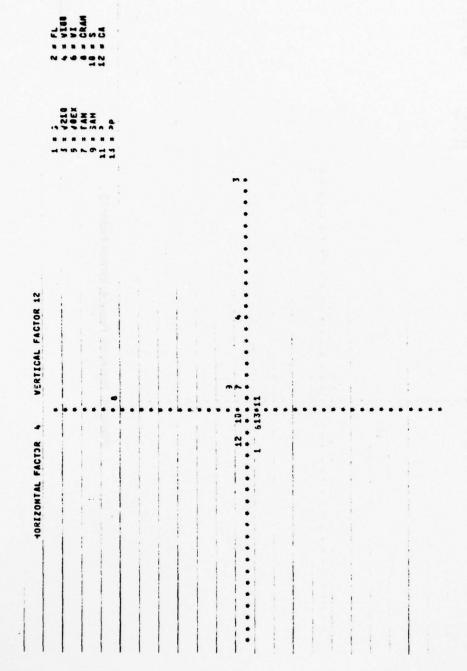


Figure 43. Horizontal Factor 4; Vertical Factor 12.

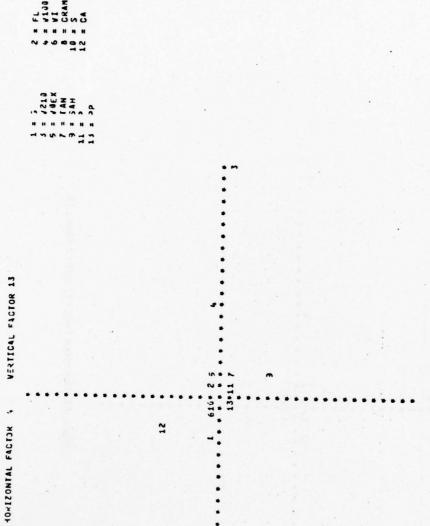


Figure 44. Horizontal Factor 4; Vertical Factor 13.

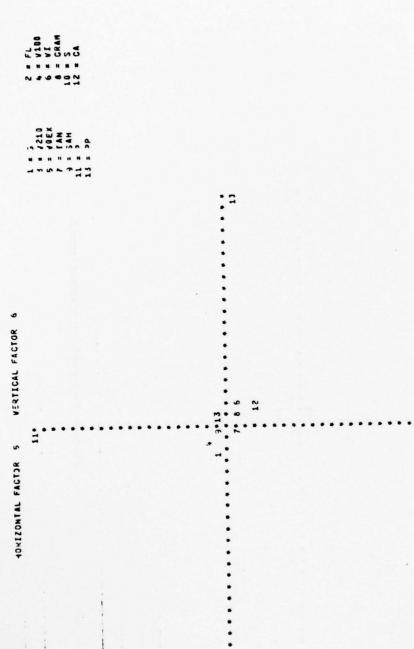


Figure 45. Horizontal Factor 5; Vertical Factor 6.

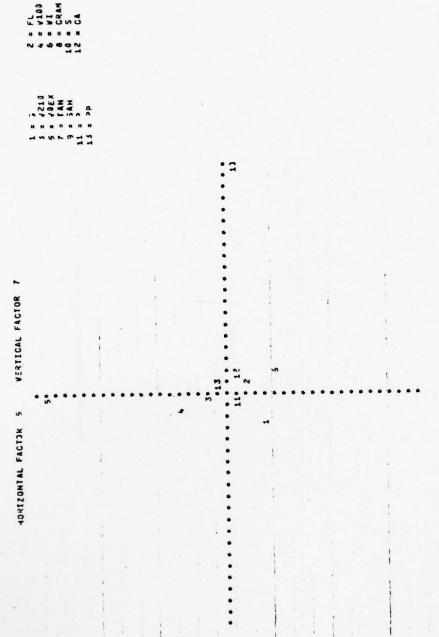
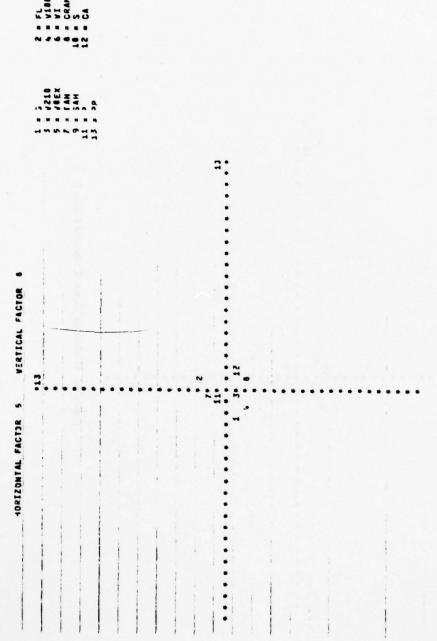
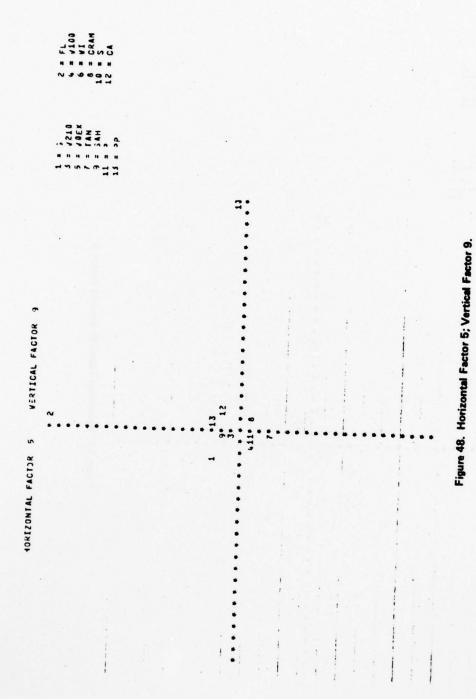


Figure 46. Horizontal Factor 5; Vertical Factor 7.





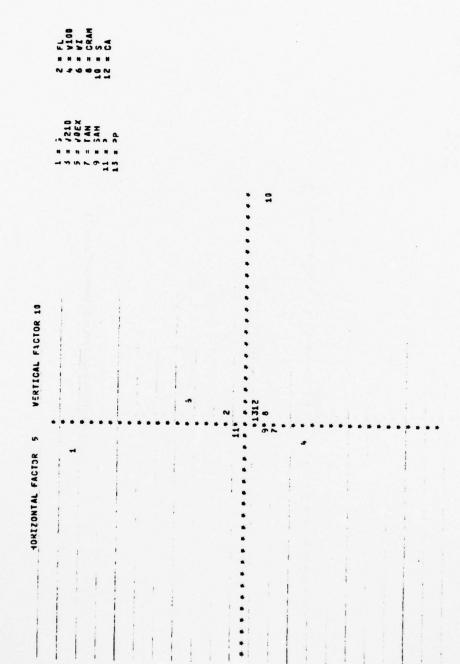
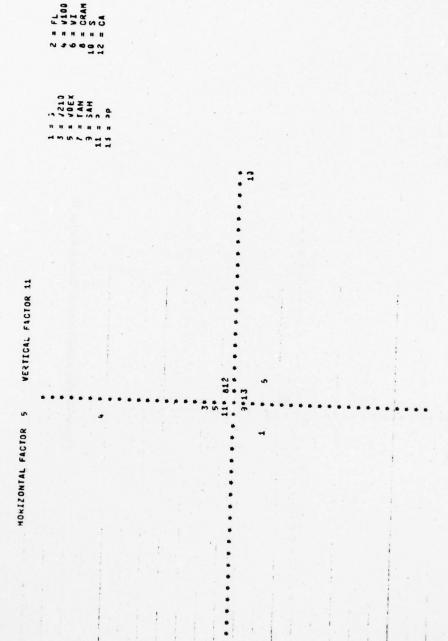
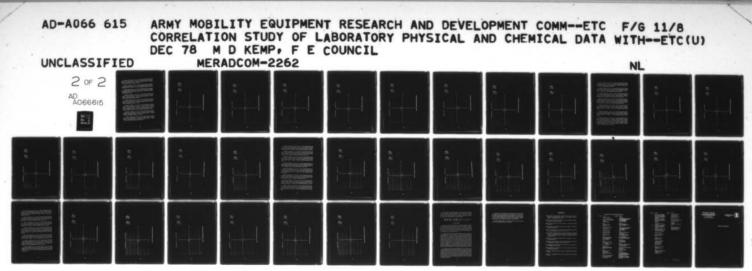
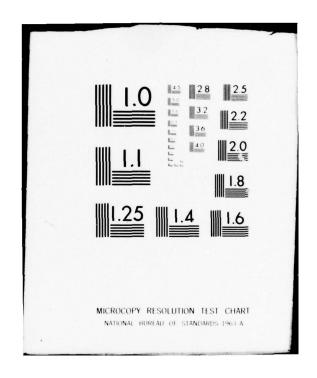


Figure 49. Horizontal Factor 5; Vertical Factor 10.





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In Figure 51, variables 1, 9, 4, 7, 12, 11, 13, and 6 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variable 8 loads high on factor 12. Variables 2, 3, and 5 have insignificant loadings on both factors.

In Figure 52, variables 1, 2, 4, 5, 6, 11, and 13 cluster and are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 10 loads high on factor 5. Variables 3, 7, and 8 show insignificant loading on both factors.

In Figure 53, variables 3, 8, 13, 12, 10, 9, and 2 cluster and are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. Variable 5 loads high on factor 7. Variable 7 shows insignificant loading on both factors.

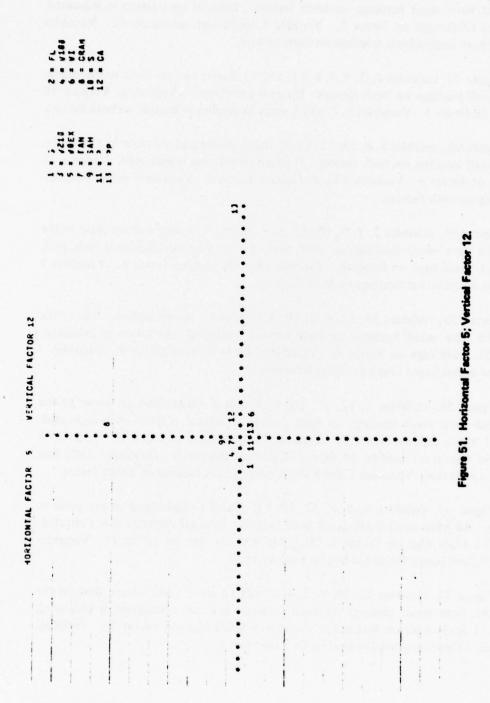
In Figure 54, variables 2, 7, 9, 10, 12, 6, 3, 8, and 4 cluster and are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. Variable 13 loads high on factor 8. Variables 1 and 5 show insignificant loadings on both factors.

In Figure 55, variables 13, 12, 6, 9, 10, 3, 8, 4, and 7 cluster and are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. Variable 2 loads high on factor 9. Variables 1 and 5 show insignificant loadings on both factors.

In Figure 56, variables 2, 12, 13, 10, 9, 7, and 3 cluster and are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 1 loads high on factor 10. Variable 11 loads high on factor 6. Variables 6 and 4 have significant loading on factor 10 and are negatively correlated. Only one grouping is indicated. Variables 5 and 8 show insignificant loading on either factor.

In Figure 57, variables 3, 5, 8, 12, 10, 13, 6, and 1 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. Variable 4 loads high on factor 11. Variables 2, 7, and 9 show insignificant loading on both factors.

In Figure 58, variables 12, 10, 9, 3, 4, 6, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. Variable 8 loads high on factor 12. Variables 1, 2, 5, and 7 show insignificant loading on either factor.



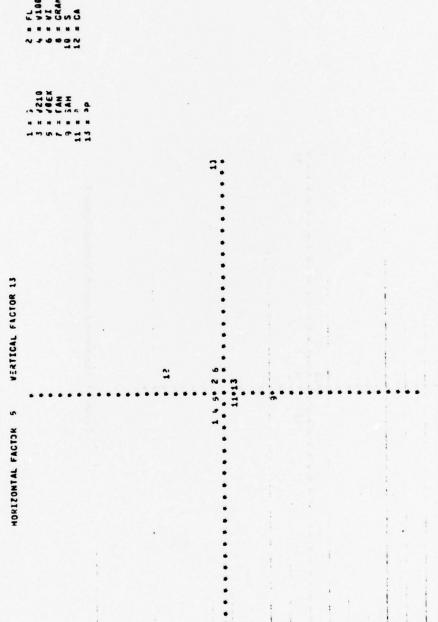


Figure 52. Horizontal Factor 5; Vertical Factor 13.

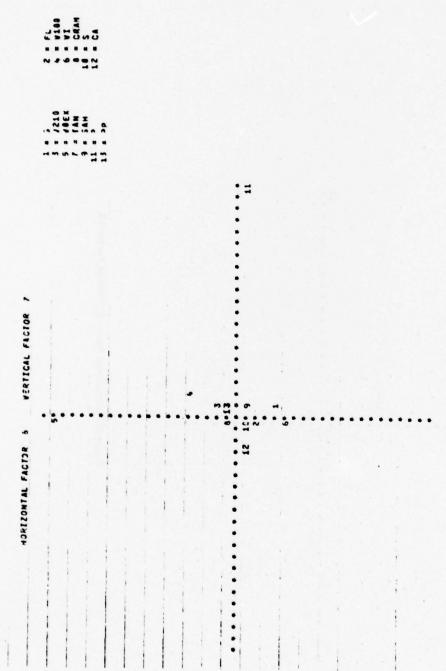
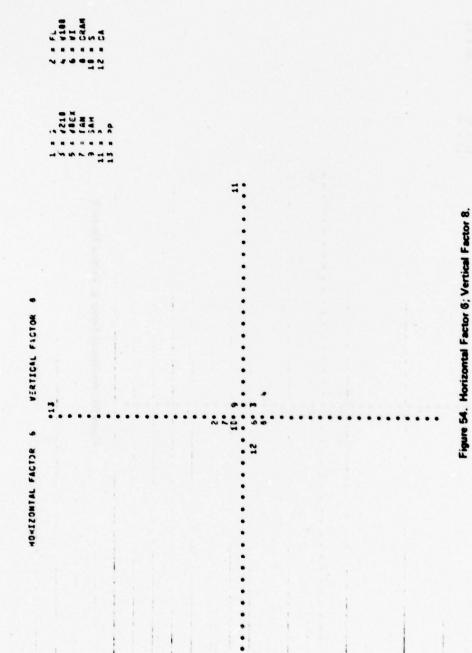


Figure 53. Horizontal Factor 6; Vertical Factor 7.



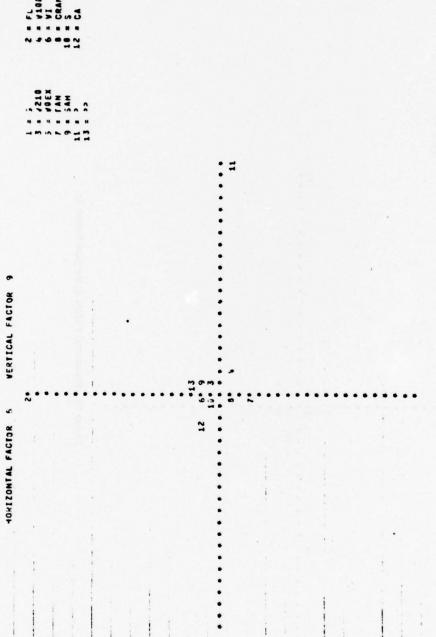
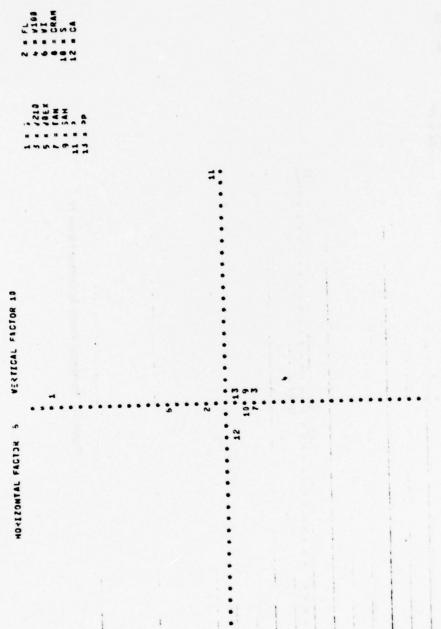


Figure 55. Horizontal Factor 6; Vertical Factor 9.



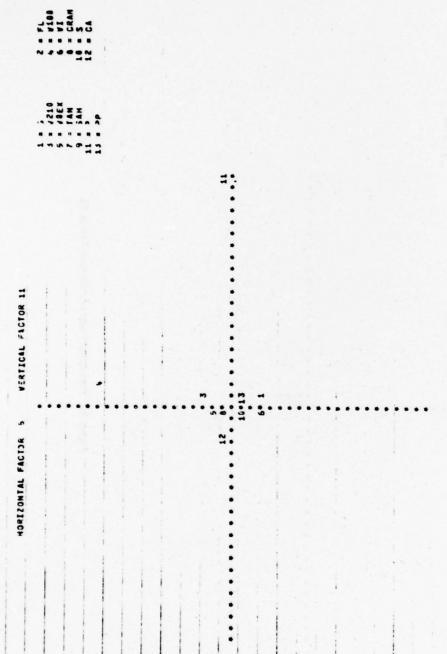
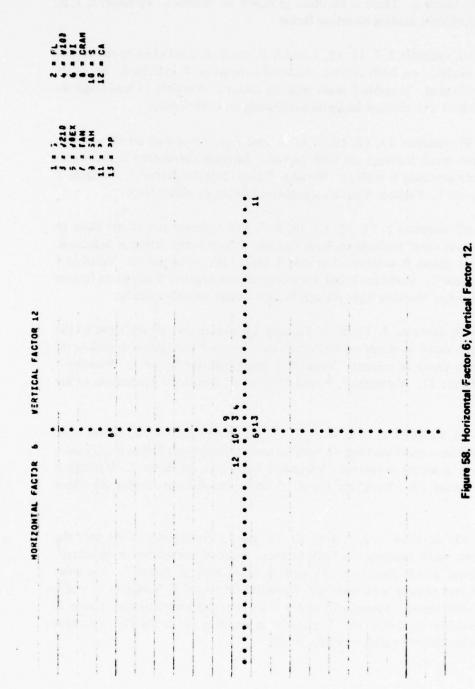


Figure 57. Horizontal Factor 6; Vertical Factor 11.



In Figure 59, variables 10, 1, 4, 8, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. Variable 11 loads high on factor 6. There is no other grouping of variables. Variables 2, 3, 5, and 7 have no significant loading on either factor.

In Figure 60, variables 2, 7, 11, 12, 3, and 8 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other discrete set is indicated. Variable 5 loads high on factor 7. Variable 13 loads high on factor 8. Variables 9 and 10 show insignificant loading on both factors.

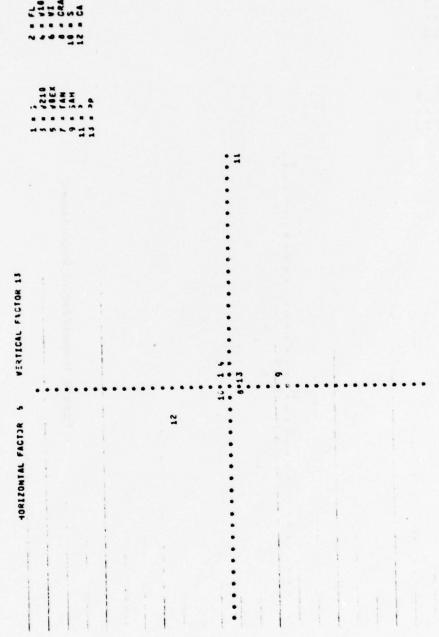
In Figure 61, variables 13, 12, 10, 3, 11, 8, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other discrete grouping is evident. Variable 5 loads high on factor 7. Variable 2 loads high on factor 9. Variable 9 has no significant loading on either factor.

In Figure 62, variables 2, 11, 12, 13, 10, 8, 7, and 3 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other discrete group is evident. Variable 1 loads high on factor 10. Variable 5 loads high on factor 7. Variables 6 and 4 have significant negative loadings on factors 10 and 7 respectively. Variable 9 has no significant loadings on either factor.

In Figure 63, variables 3, 12, 8, 2, 10, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other discrete group is evident. Variable 5 loads high on factor 7. Variable 4 loads high on factor 11. Variables 7, 9, and 11 have no significant loading on either factor.

In Figure 64, variables 1, 2, 3, 4, 6, 9, 11, 12, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other discrete grouping is evident. Variable 5 loads high on factor 7. Variable 8 loads high on factor 12. Variables 7 and 10 show insignificant loading on either factor.

In Figure 65, variables 1, 2, 3, 4, 6, 10, 11, and 13 cluster and all are near the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is indicated here. Variable 5 loads high on factor 7. Variables 4, 12, 6, and 9 load equally with variable 12 positive on factor 7. Variables 12 and 9 show negative correlation. Variables 6 and 4 show negative correlation on factor 7. Variable 4 is positive on factor 13. Variables 6 and 8 show insignificant loading on either factor.



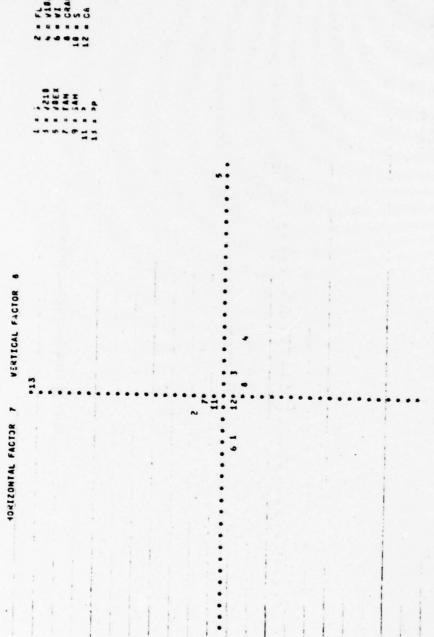
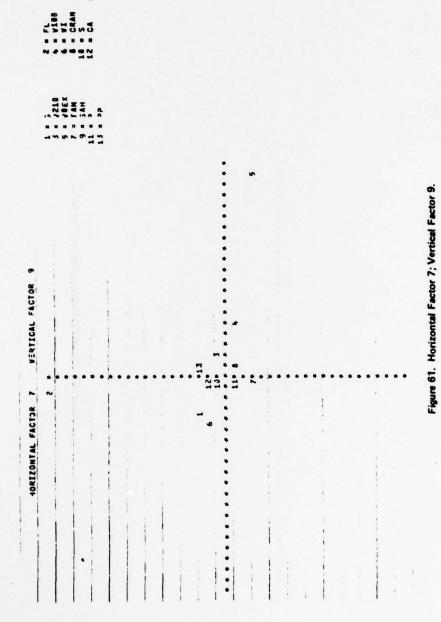


Figure 60. Horizontal Factor 7; Vertical Factor 8.



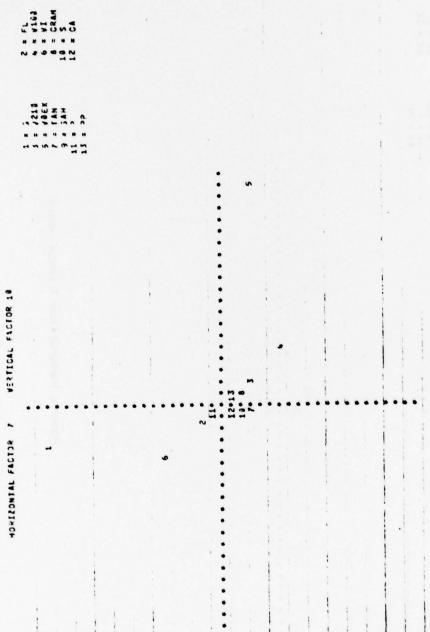


Figure 62 Horizontal Factor 7; Vertical Factor 10.

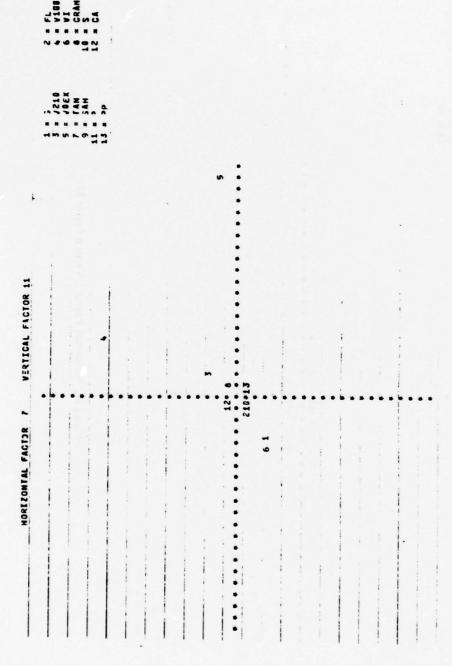


Figure 63. Horizontal Factor 7; Vertical Factor 11.

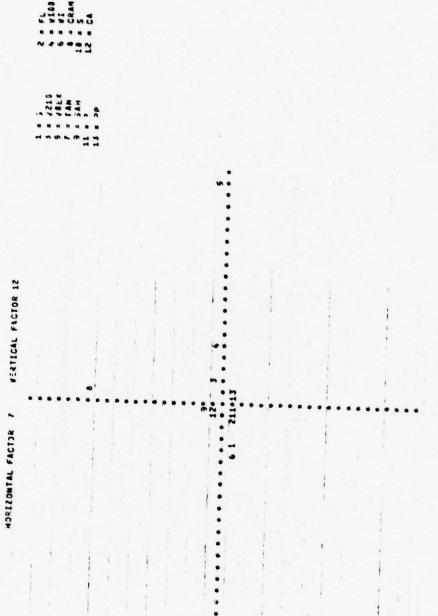
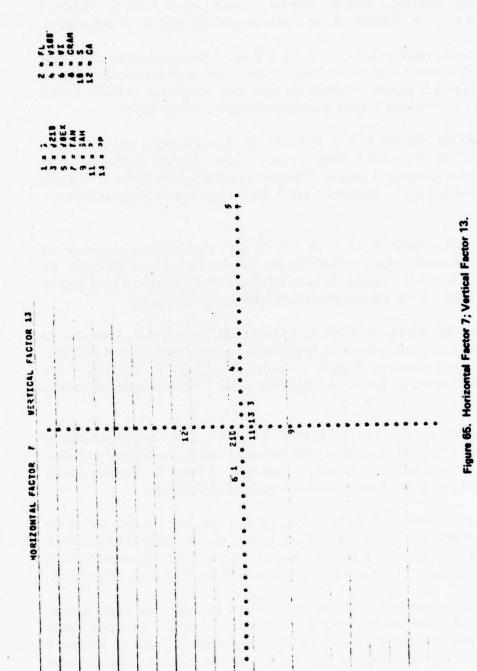


Figure 64. Horizontal Factor 7; Vertical Factor 12.



In Figure 66, variables 1, 12, 9, 3, 10, 8, 11, 5, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 13 loads high on factor 8. Variable 2 loads high on factor 9. Variables 4 and 6 show insignificant loadings on either factor.

In Figure 67, variables 2, 11, 12, 8, 10, 3, 5, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 13 loads high on factor 8. Variable 1 loads high on factor 10. Variable 9 shows insignificant loading on either factor.

In Figure 68, variables 3, 5, 7, 8, 12, 11, 10, 2, and 6 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 13 loads high on factor 8. Variable 4 loads high on factor 11. Variables 1 and 9 show insignificant loading on both factors.

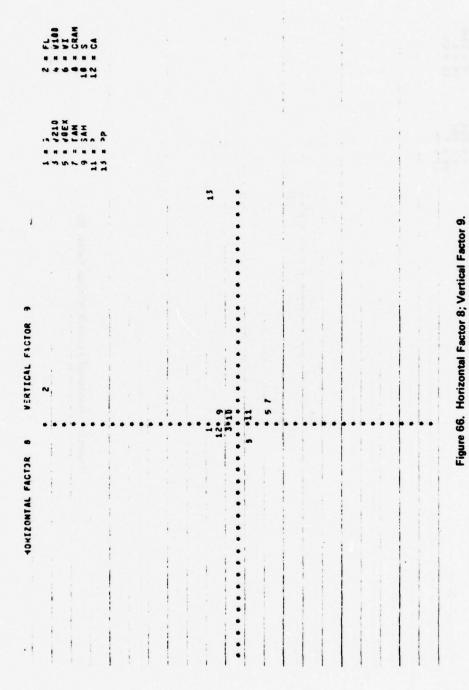
In Figure 69, variables 4, 12, 9, 10, 7, 6, 11, and 2 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 13 loads high on factor 8. Variable 8 loads high on factor 12. Variables 3 and 5 show insignificant loadings on either factor.

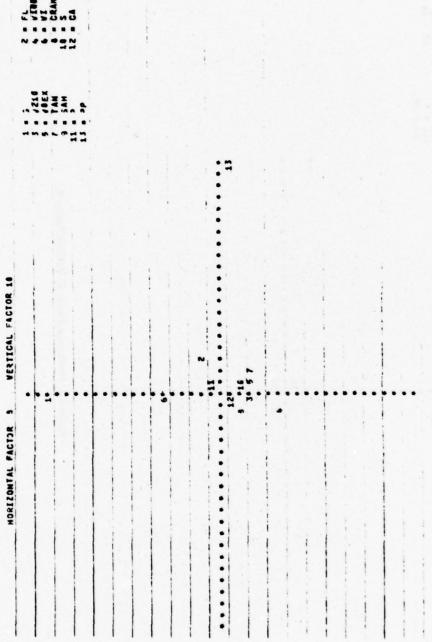
In Figure 70, variables 4, 6, 10, 2, 8, 3, 11, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 13 loads high on factor 8. Variables 12 and 9 have modest loading on factor 13. Variables 1 and 5 have insignificant loadings on either factor.

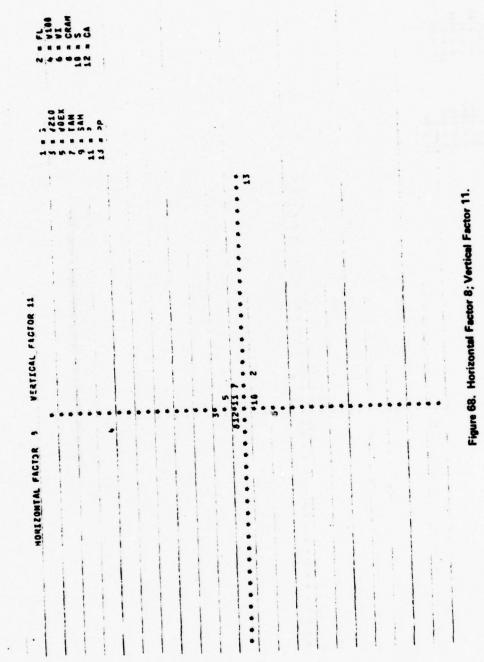
In Figure 71, variables 11, 12, 13, 10, 9, 8, 7, and 3 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 2 loads high on factor 9. Variable 1 loads high on factor 10. Variable 5 has insignificant loading on either factor.

In Figure 72, variables 3, 5, 7, 11, 12, 10, 9, 13, 6, and 1 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 2 loads high on factor 9. Variable 4 loads high on factor 11. Variable 8 shows insignificant loading on either factor.

In Figure 73, variables 9, 7, 4, 10, 12, 11, 6, and 13 cluster and all are close to to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 2 loads high on factor 9. Variable 8 loads high on factor 12. Variables 1, 3, and 5 show insignificant loadings on either factor.







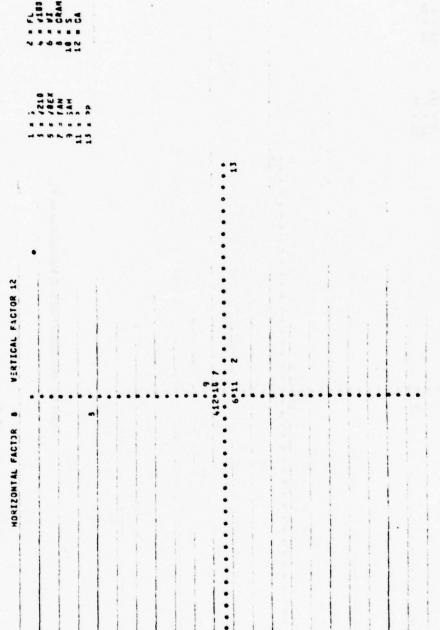
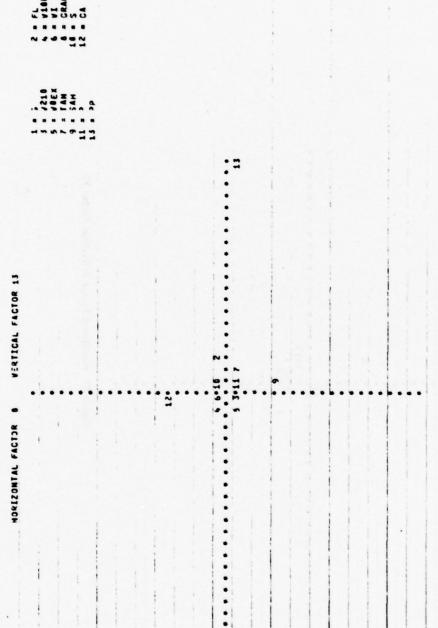


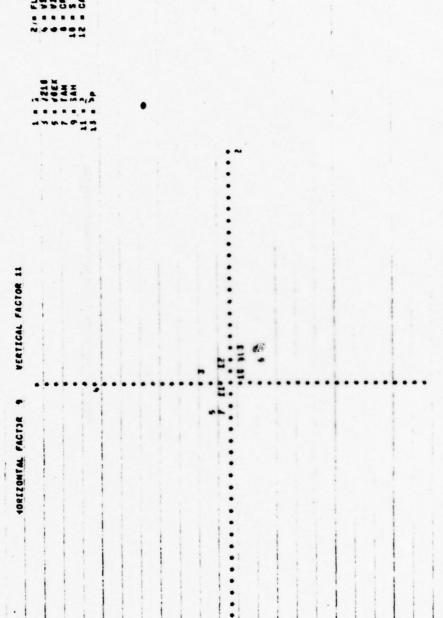
Figure 69. Horizontal Factor 8; Vertical Factor 12.



!

Figure 70. Horizontal Factor 8; Vertical Factor 13.

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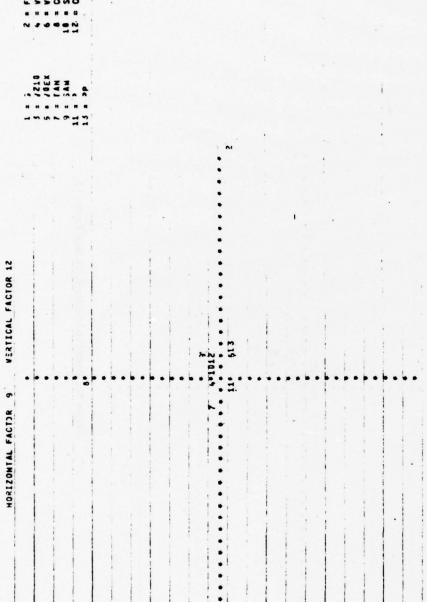


Figure 73. Horizontal Factor 9; Vertical Factor 12.

In Figure 74, variables 5, 4, 10, 6, 1, 7, 11, 3, and 13 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 2 loads high on factor 9. Variables 12 and 9 (negative) load on factor 13 with a negative correlation. Variable 8 shows insignificant

In Figure 75, variables 3, 5, 7, 8, 12, 11, 10, 13, and 2 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 1 loads high on factor 10. Variable 4 loads high on factor 11. Variable 9 shows insignificant loading on either factor.

loading on either factor.

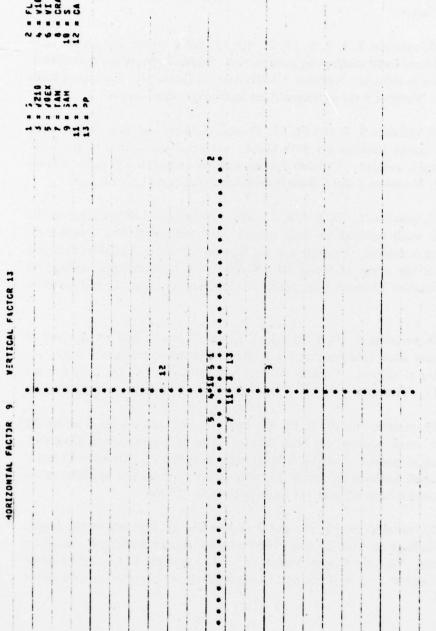
In Figure 76, variables 9, 7, 10, 12, 13, 11, and 2 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 1 loads high on factor 10. Variable 8 loads high on factor 12. Variables 3 and 5 show insignificant loading on either factor.

In Figure 77, variables 5, 10, 2, 7, 8, 13, and 11 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 1 loads high on factor 10. Variables 6, 2, and 4 have loadings at the origin of factor 10. Variable 3 has insignificant loadings on either factor. Variables 12 and 9 have significant loadings on factor 13 and correlate negatively.

In Figure 78, variables 6, 10, 5, 13, 11, 9, 3, and 12 cluster and are all close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 4 loads high on factor 11. Variable 8 loads high on factor 12. Variables 1, 2, and 7 have insignificant loadings on either factor.

In Figure 79, variables 6, 10, 5, 13, 11, and 3 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 4 loads high on factor 11. Variables 12 and 9 (negative) have small loadings on factor 13 with variable 9 having a negative value. Variables 1, 2, 7, and 8 have insignificant loadings on either factor.

In Figure 80, variables 6, 10, 13, and 7 cluster and all are close to the origin. All have small loadings on both factors. Internal correlation is indicated. No other grouping is evident. Variable 8 loads high on factor 12. Variable 12 has small loading on factor 13. Variables 1, 2, 3, 4, 5, and 11 have insignificant loadings on both factor 13 and factor 12.



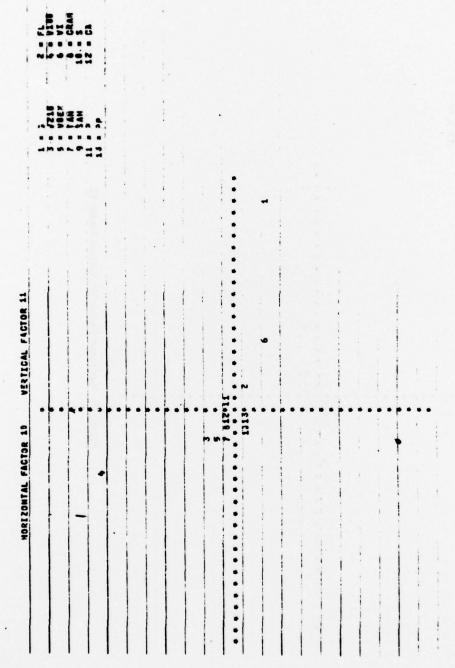


Figure 75. Horizontal Factor 10; Vertical Factor 11.

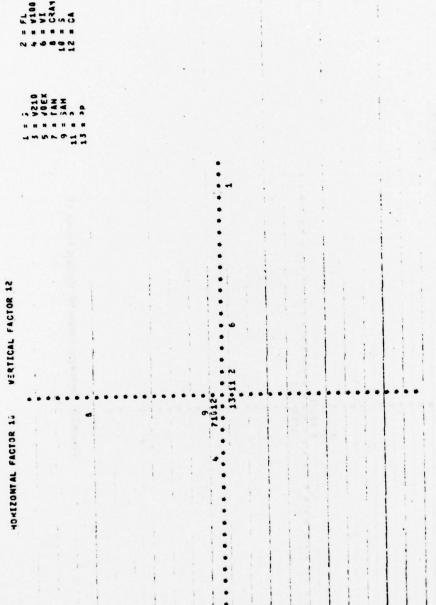


Figure 76. Horizontal Factor 10; Vertical Factor 12.

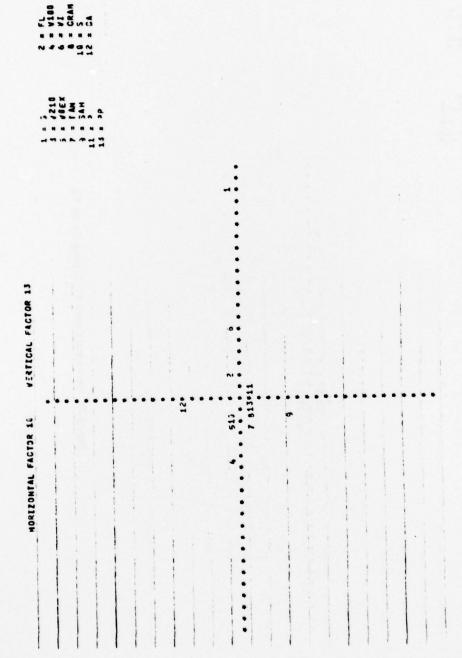


Figure 77. Horizontal Factor 10; Vertical Factor 13.

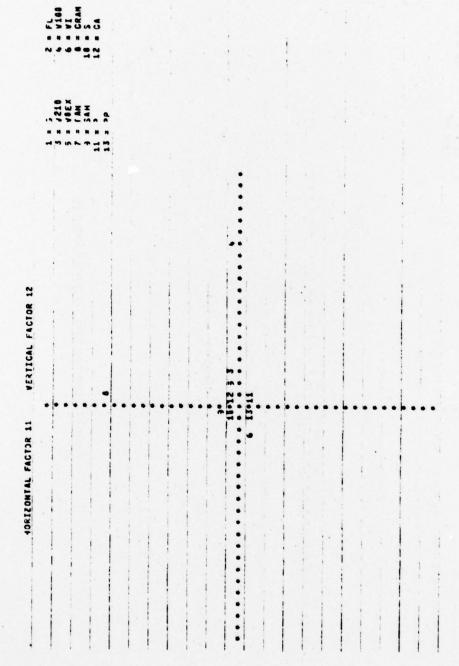
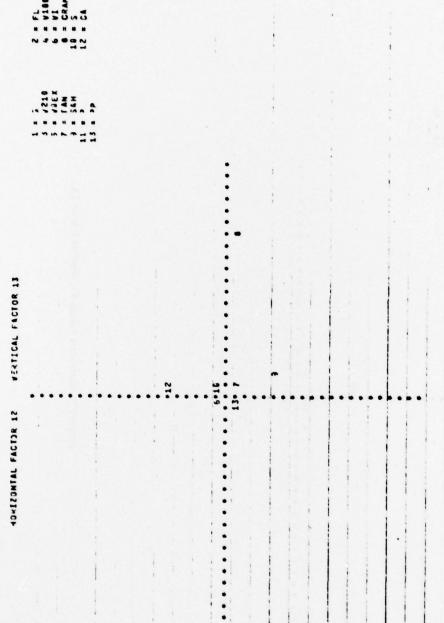


Figure 78. Horizontal Factor 11; Vertical Factor 12.

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Figure 79. Horizontal Factor 11; Vertical Factor 13.



Varimax rotation as discussed analytically above represents one factoring solution applied to the data by the SPSS subprogram. In varimax application, the criterion centers on simplying the columns of the factor matrix. A simple factor is defined as one with only 1s and 0s in the column. This simplication amounts to maximizing the variance of the squared loadings in each column according to

$$n\sum_{p=1}^{n}\sum_{j=1}^{n}\left(\frac{ajp}{hj}\right)^{4}-\sum_{p=1}^{n}\left(\sum_{j=1}^{n}\frac{a^{2}jp}{h^{2}j}\right)^{2}$$
 maximum.

V. CONCLUSIONS

An overall look has been made at laboratory chemical and physical data obtained on 80 lubricating oils meeting the requirements of Specification MIL-L-2104 employing an SPSS statistical package and a CDC computer. The purpose of this effort was to seek internal correlations among the data and dynamometer results and field performance and to seek ways to relate laboratory data and field performance. Out of a possible 26 pieces of analytical data collected for each of the 80 samples, 13 pieces of information were selected for scrutiny.

It was found that, overall, the data exhibited substantial variance, departed from a normal distribution in all cases, and showed, in general, a lack of internal correlation among the data items. There was exhibited, however, significant correlations between selected pairs of data. Sulphated ash vs calcium, sulphated ash vs carbon residue, and carbon residue vs calcium showed favorable Pearson's correlation. From the unmatched, unrotated, factor matrix, flash point was influenced by calcium, sulphated ash, and carbon residue. Flash point was negatively influenced by gravity. Viscosity at 210°F was strongly influenced, or vice versa, by total acid number, flash point, and phosphorus. Negligible influence was noted for flash point or viscosity at 0 (extrapolated) and viscosity index, etc. Other examples of paired correlation were indicated by the data. Significant in the observations was the fact that about 80% of the total variance of the observations was attributed to only three analytical items — flash point, gravity, and viscosity measurements. The importance of this deserves further scrutiny.

The statistical package, SPSS, that was employed allows the exhibition of the orthogonal rotation of the data in graphical presentation. When this is accomplished, certain groupings of the data become evident. These groupings suggest internal correlation of groups of data and could point the way to considerable data-reductions possibilities. Dynamometer and field results were not available in this study, but the possibility exists that if these results were included along with the graphical presentations, information on the relationships between laboratory, chemical, and physical observations and dynamometer and fuel observations could be obtained. The graphical presentations are included.

The application of these statistics to selected chemical and physical data obtained from lubricating oils has been performed in a very preliminary way. The results so far only suggest certain correlations and data-reduction possibilities. To be more meaningful, a more complete inclusion of the data on a greater number of samples is warranted. The uniqueness of the distributions, the failure of the distributions to approach normality, and the apparent negative correlations need further explanation.

The SPSS statistical package or some variation does seem to offer a possible method for the accomplishment of the task undertaken.

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